

Seminarium Astrofizyczne  
WFAIS UJ oraz Komisji Astrofizyki PAU  
Kraków, 15.01.2020

# Soczewki grawitacyjne:

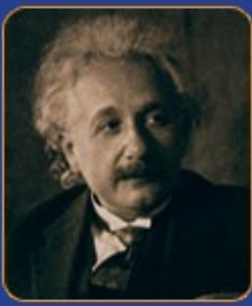
od ekspedycji Eddingtona do pierwszego obrazu horyzontu czarnej  
dziury

**Marek Biesiada**

Zakład Astrofizyki  
Narodowe Centrum Badań Jądrowych  
Warszawa



NATIONAL CENTRE  
FOR NUCLEAR RESEARCH  
ŚWIERK



# THE INTERNATIONAL SOCIETY ON GENERAL RELATIVITY & GRAVITATION

Rok 2019 kolejna 100 rocznica

związana z Ogólną Teorią Względności

29 maja 1919 ekspedycja Eddingtona

28 lipca 1919 **powstaje IAU** – komitet C1:  
Teorii względności – przewodniczy mu  
Sir Arthur Eddington

Listopad 1919 – wyniki ekspedycji  
Eddingtona ogłoszone drukiem

# Historycznie:

John Michell (1724-1793) w liście do Henry'ego Cavendisha (1731-1810) [niezależnie Soldner 1801]

- założmy, że światło składa się z cząstek
- w polu grawitacyjnym Słońca cząstka światła doznaje przyspieszenia

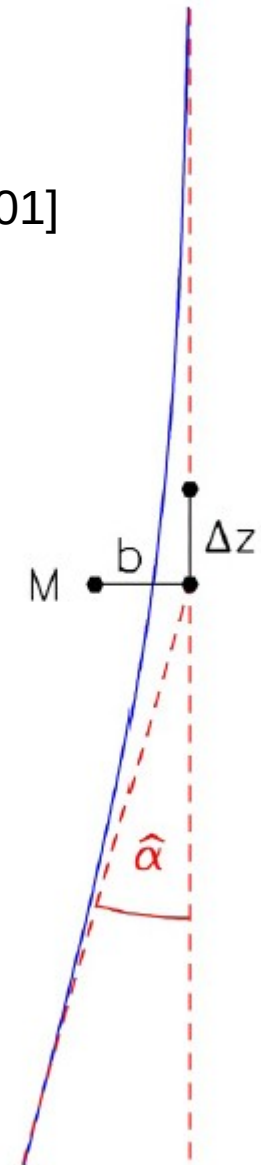
$$\frac{d^2\vec{r}}{dt^2} = -\frac{Gm\vec{r}}{r^3}$$

- ogólnie trajektoria jest jednym z przekrojów stożkowych (elipsa, parabola, hiperbola)
- dla światła będzie to hiperbola ( $c \gg V_{\text{esc}}$ )
- stąd wyliczamy
- dla promienia świetlnego stycznego do brzegu tarczy Słońca

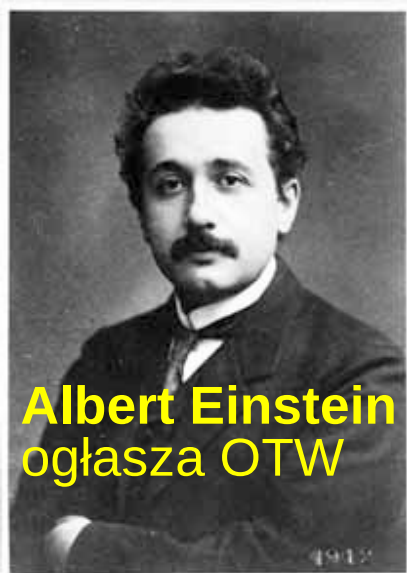
$$\alpha = \frac{2GM}{c^2 b}$$

$$\alpha = \frac{2GM}{c^2 R} = 0''.875$$

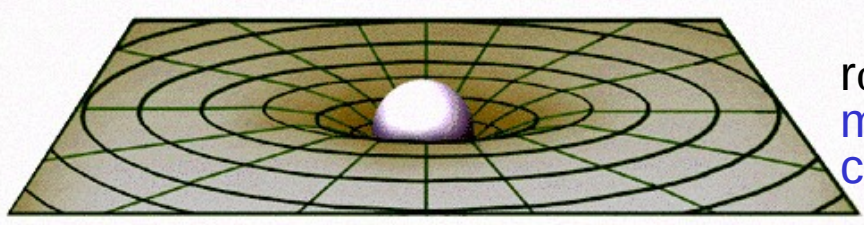
$$m = M_{\odot} = 1.989 \times 10^{30} \text{kg}$$
$$R = R_{\odot} = 6.96 \times 10^8 \text{m}$$



turbulencja atmosfery  
„seeing” 0.5 – 1.”



**Albert Einstein**  
ogłasza OTW



równania pola Einsteina – jak materia zakrzywia czasoprzestrzeń

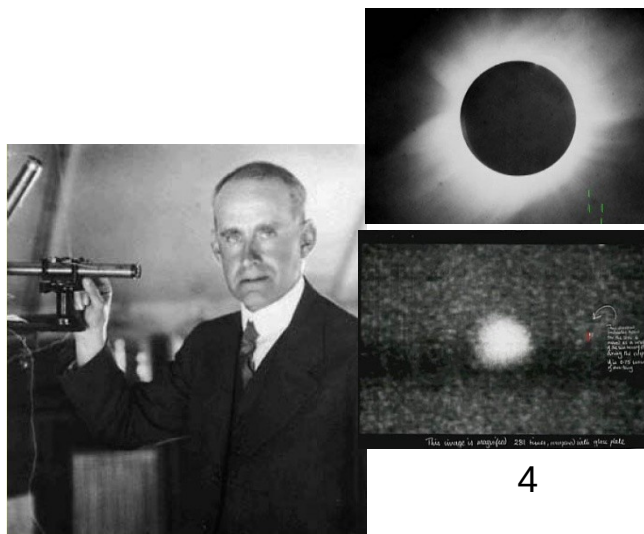
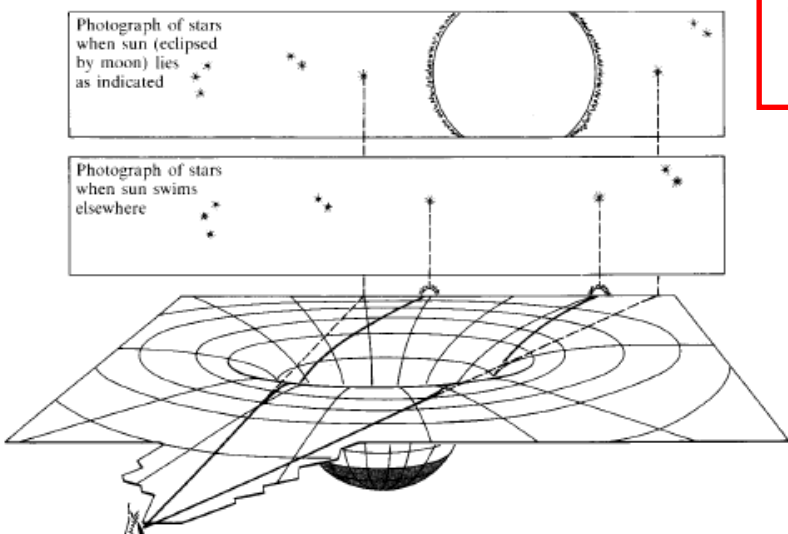
w zakrzywionej czasoprzestrzeni ruch swobodny ciał odbywa się po geodetykach (tj. najkrótszych drogach)

$$G_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

Ugięcie światła w pobliżu brzegu tarczy Słońca Zakrzywienie czasoprzestrzeni czują nie tylko ciała masywne, ale także światło !

29.V.1919  
**Sir Arthur Eddington**  
Całkowite zaćmienie Słońca na tle Hlad

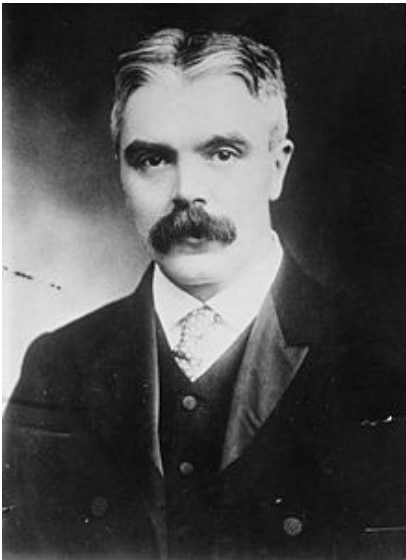
$$\alpha = \frac{4GM}{c^2 R} = 1''.75$$







Sir Arthur Stanley Eddington  
1882 - 1944



Sir Frank Watson Dyson  
1868 - 1939

IX. *A Determination of the Deflection of Light by the Sun's Gravitational Field, from Observations made at the Total Eclipse of May 29, 1919.*

By Sir F. W. DYSON, F.R.S., Astronomer Royal, Prof. A. S. EDDINGTON, F.R.S., and Mr. C. DAVIDSON.

(Communicated by the Joint Permanent Eclipse Committee.)

Received October 30,—Read November 6, 1919.

Historyczna praca

[PLATE 1.]

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I. PURPOSE OF THE EXPEDITIONS.

1. THE purpose of the expeditions was to determine what effect, if any, is produced by a gravitational field on the path of a ray of light traversing it. Apart from possible surprises, there appeared to be three alternatives, which it was especially desired to discriminate between—

- (1) The path is uninfluenced by gravitation.
- (2) The energy or mass of light is subject to gravitation in the same way as ordinary matter. If the law of gravitation is strictly the Newtonian law, this leads to an apparent displacement of a star close to the sun's limb amounting to  $0''\cdot87$  outwards.
- (3) The course of a ray of light is in accordance with EINSTEIN'S generalised relativity theory. This leads to an apparent displacement of a star at the limb amounting to  $1''\cdot75$  outwards.

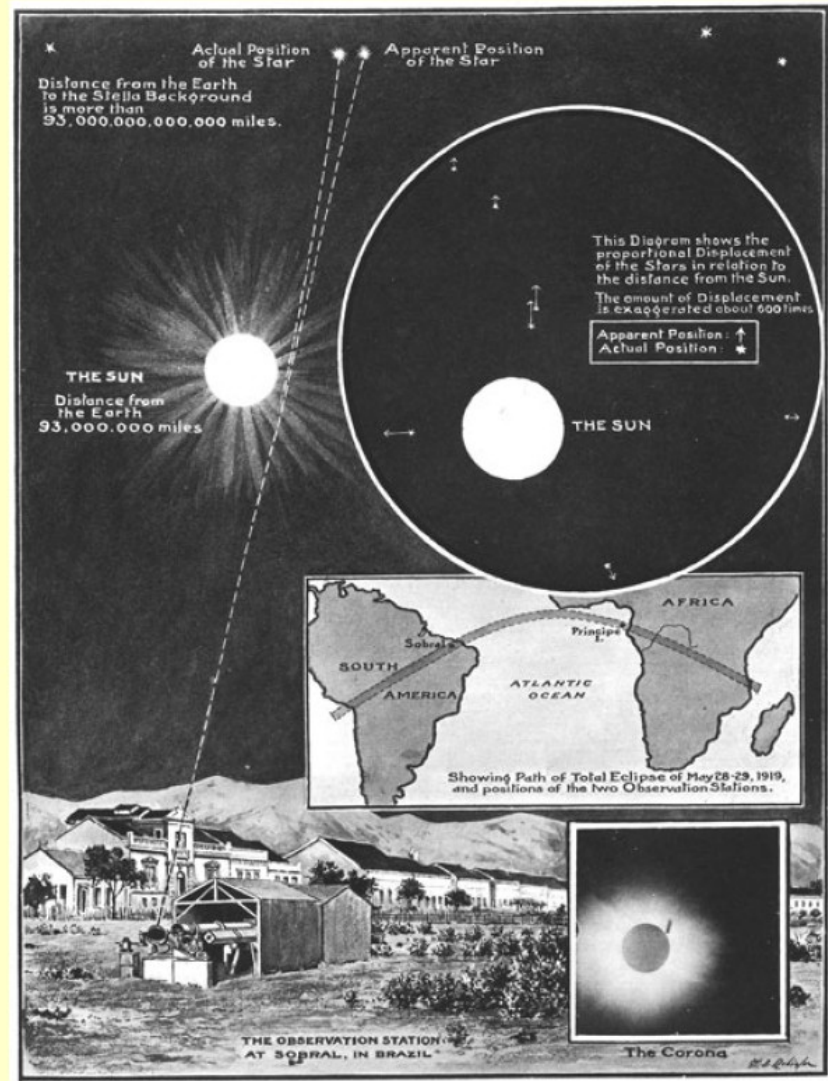
In either of the last two cases the displacement is inversely proportional to the distance of the star from the sun's centre, the displacement under (3) being just double the displacement under (2).

It may be noted that both (2) and (3) agree in supposing that light is subject to gravitation in precisely the same way as ordinary matter. The difference is that, whereas (2) assumes the Newtonian law, (3) assumes EINSTEIN'S new law of gravitation. The slight

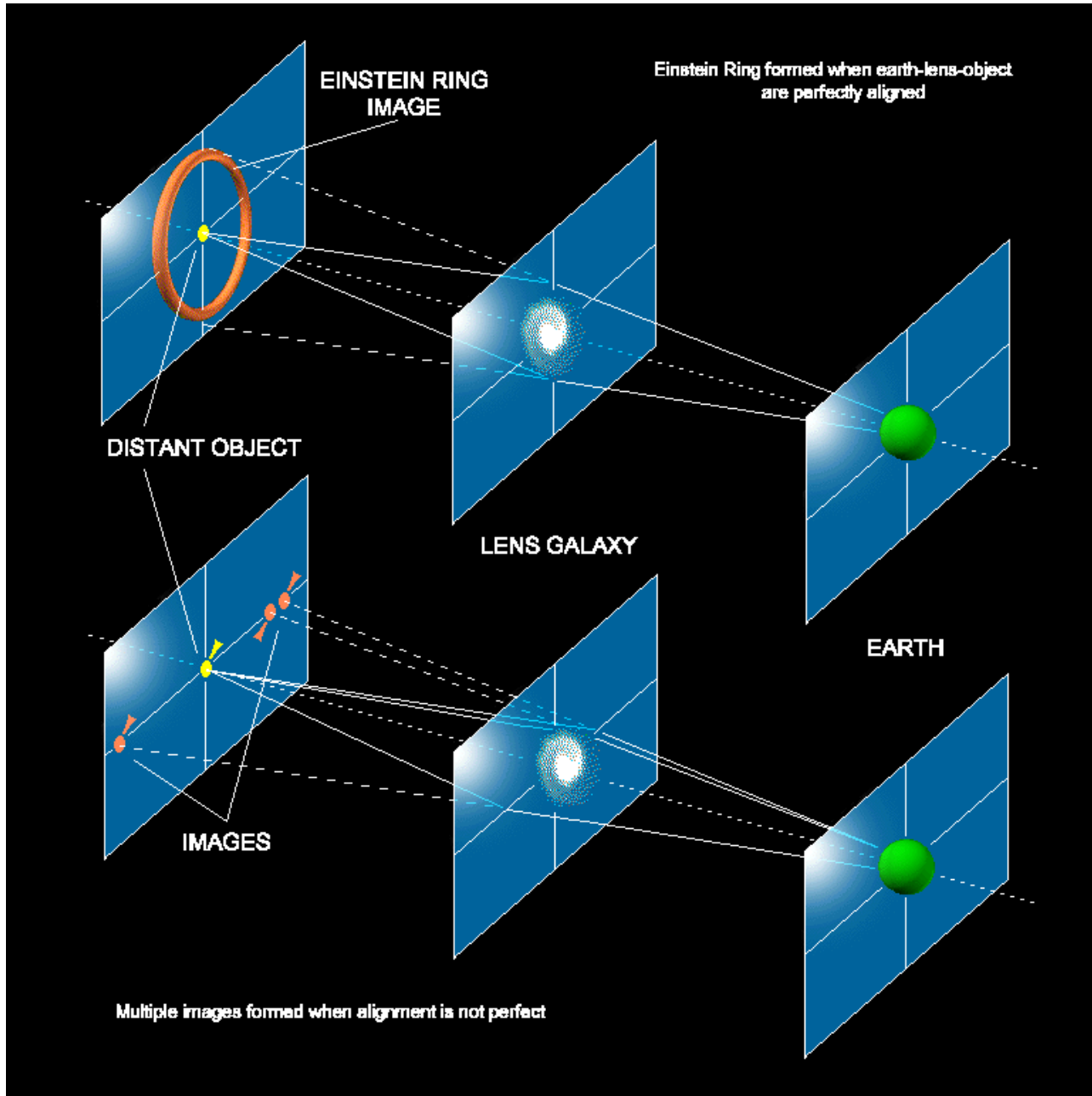
# Obserwacje Eddingtona

The results obtained by the British expeditions to observe the total eclipse of the sun last May verified Professor Einstein's theory that light is subject to gravitation. Writing in our issue of November 15 [1919], **Dr. A.C. Crommelin, one of the British observers, said:** "The eclipse was specially favourable for the purpose, there being no fewer than twelve fairly bright stars near the limb of the sun. The process of observation consisted in taking photographs of these stars during totality, and comparing them with other plates of the same region taken when the sun was not in the neighbourhood. Then if the starlight is bent by the sun's attraction, the stars on the eclipse plates would seem to be pushed outward compared with those on the other plates. The second Sobral camera and the one used at Principe agree in supporting Einstein's theory. It is of profound philosophical interest. Straight lines in Einsteins space cannot exist; they are parts of gigantic curves."

Einstein staje się celebrytą !



Illustrated London News of November 22, 1919.



## Konsekwencja:

soczewkowanie  
grawitacyjne

Einstein – pierścień  
Einsteina

$$\theta_E = \sqrt{\frac{4GM}{c^2} \frac{D_{LS}}{D_L D_S}}$$

Eddington 1920

idea wielokrotnych  
obrazów



# Soczewkowanie grawitacyjne

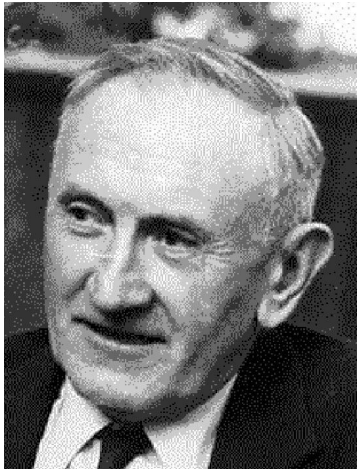
- Einstein sceptyczny co do obserwowalności efektu

soczewki o masach rzędu masy Słońca  $1 M_{\odot}$  przy odległościach wzajemnych typowych dla Galaktyki 5 – 10 kpc mają promień Einsteina rzędu  $0''.001$  – **nieobserwowalne !**

- Zwicky 1937 (!) galaktyki w roli soczewek

**Galaktyki** mają masy rzędu  $10^{11} - 10^{12} M_{\odot}$   
ich wzajemne odległości to 10 Mpc – 1 Gpc  
daje to promień Einsteina rzędu **1''**.

**To już można zobaczyć !**



Fritz Zwicky  
1898 - 1974



### LENS-LIKE ACTION OF A STAR BY THE DEVIATION OF LIGHT IN THE GRAVITATIONAL FIELD

SOME time ago, R. W. Mandl paid me a visit and asked me to publish the results of a little calculation, which I had made at his request. This note complies with his wish.

The light coming from a star  $A$  traverses the gravitational field of another star  $B$ , whose radius is  $R_0$ . Let there be an observer at a distance  $D$  from  $B$  and at a distance  $x$ , small compared with  $D$ , from the extended central line  $\overline{AB}$ . According to the general theory of relativity, let  $\alpha_0$  be the deviation of the light ray passing the star  $B$  at a distance  $R_0$  from its center.

For the sake of simplicity, let us assume that  $\overline{AB}$  is large, compared with the distance  $D$  of the observer from the deviating star  $B$ . We also neglect the eclipse (geometrical obscuration) by the star  $B$ , which indeed is negligible in all practically important cases. To permit this,  $D$  has to be very large compared to the radius  $R_0$  of the deviating star.

It follows from the law of deviation that an observer situated exactly on the extension of the central line  $\overline{AB}$  will perceive, instead of a point-like star  $A$ , a luminous circle of the angular radius  $\beta$  around the center of  $B$ , where

$$\beta = \sqrt{\alpha_0 \frac{R_0}{D}}$$

It should be noted that this angular diameter  $\beta$  does

not decrease like  $1/D$ , but like  $1/\sqrt{D}$ , as the distance  $D$  increases.

Of course, there is no hope of observing this phenomenon directly. First, we shall scarcely ever approach closely enough to such a central line. Second, the angle  $\beta$  will defy the resolving power of our instruments. For,  $\alpha_0$  being of the order of magnitude of one second of arc, the angle  $R_0/D$ , under which the deviating star  $B$  is seen, is much smaller. Therefore, the light coming from the luminous circle can not be distinguished by an observer as geometrically different from that coming from the star  $B$ , but simply will manifest itself as increased apparent brightness of  $B$ .

The same will happen, if the observer is situated at a small distance  $x$  from the extended central line  $\overline{AB}$ . But then the observer will see  $A$  as two point-like light-sources, which are deviated from the true geometrical position of  $A$  by the angle  $\beta$ , approximately.

The apparent brightness of  $A$  will be increased by the lens-like action of the gravitational field of  $B$  in the ratio  $q$ . This  $q$  will be considerably larger than unity only if  $x$  is so small that the observed positions of  $A$  and  $B$  coincide, within the resolving power of our instruments. Simple geometric considerations lead to the expression

$$q = \frac{l}{x} \cdot \frac{1 + \frac{x^2}{2l^2}}{\sqrt{1 + \frac{x^2}{4l^2}}}$$

where

$$l = \sqrt{\alpha_0 D R_0}$$



DECEMBER 4, 1936

SCIEN

If we are interested mainly in the case  $q \gg 1$ , the formula

$$q = \frac{l}{x}$$

is a sufficient approximation, since  $\frac{x^2}{l^2}$  may be neglected.

Even in the most favorable cases the length  $l$  is only a few light-seconds, and  $x$  must be small compared with this, if an appreciable increase of the apparent brightness of  $A$  is to be produced by the lens-like action of  $B$ .

Therefore, there is no great chance of observing this phenomenon, even if dazzling by the light of the much nearer star  $B$  is disregarded. This apparent amplification of  $q$  by the lens-like action of the star  $B$  is a most curious effect, not so much for its becoming infinite, with  $x$  vanishing, but since with increasing distance  $D$  of the observer not only does it not decrease, but even increases proportionally to  $\sqrt{D}$ .

ALBERT EINSTEIN

INSTITUTE FOR ADVANCED STUDY,  
PRINCETON, N. J.



# Bohdan Paczyński (1940 – 2007)

Wybitny polski astrofizyk: [pracujący od 1981 w Princeton](#)

zapoczątkował:

[teorię ewolucji gwiazd w układach podwójnych](#)

[jako pierwszy przewidział rolę emisji fal grawitacyjnych w ewolucji ciasnych układów podwójnych](#)

[teorię dysków akrecyjnych](#)

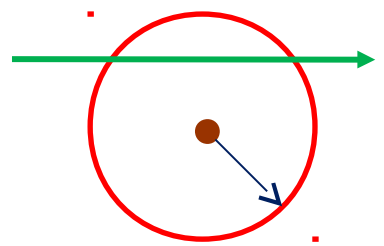
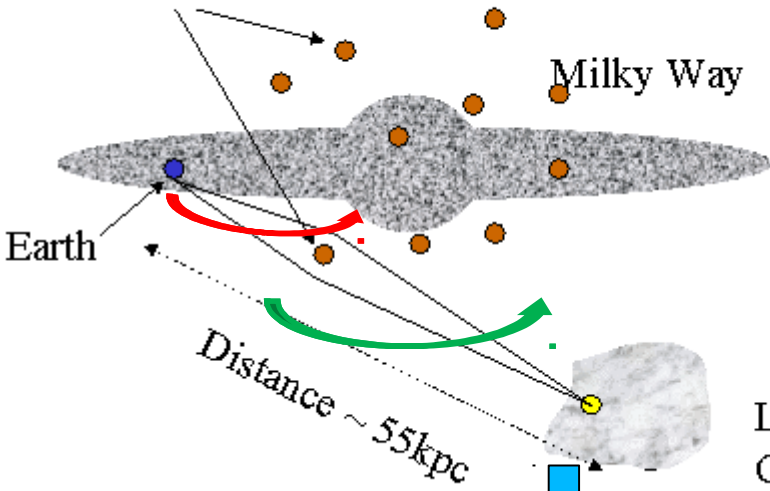
[teorię mikrosoczewkowania grawitacyjnego \(„poprawił Einsteina”\)](#)

[wyjaśnił naturę błysków gamma](#)

[rozwój „terabajtowej astronomii”](#)



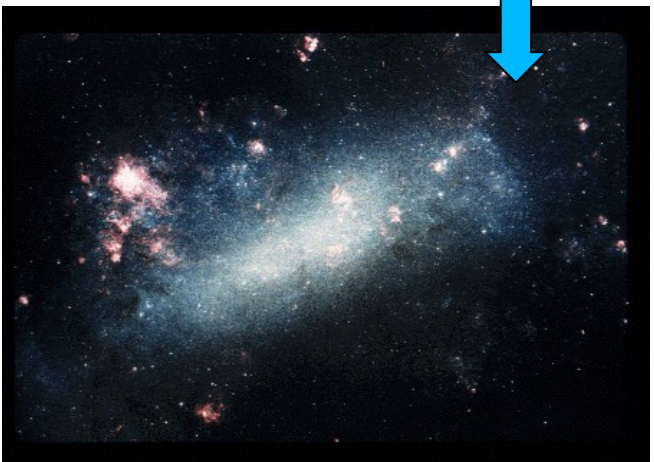
Gravitational lenses (e.g., brown dwarfs)



ruch względny  
źródła i soczewki

promień Einsteina  
soczewki

**Bohdan Paczyński 1986**  
**pomysł obserwacji**  
**mikrosoczewkowania**

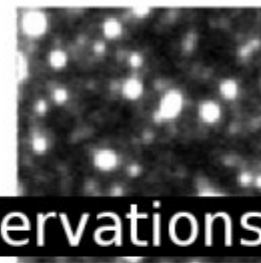
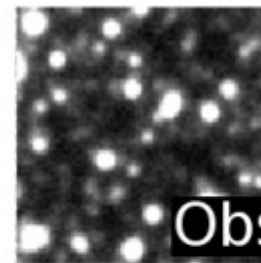
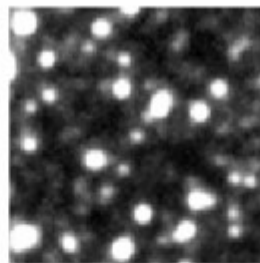
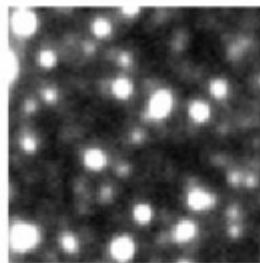
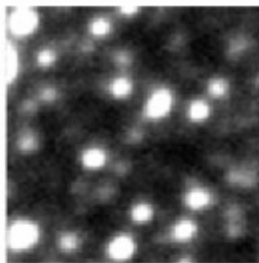
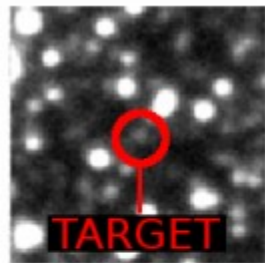
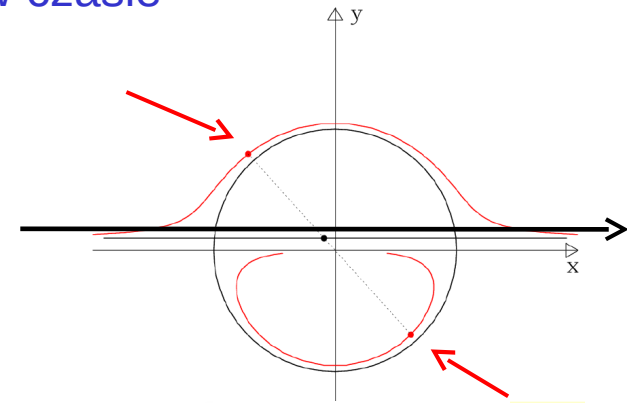


# Eksperyment OGLE

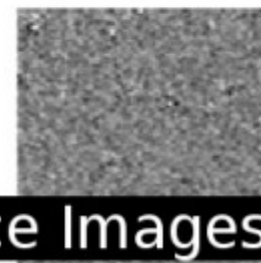
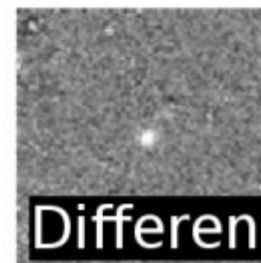
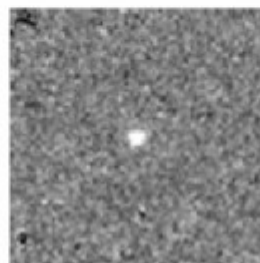
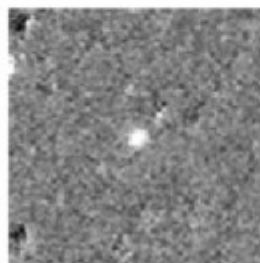
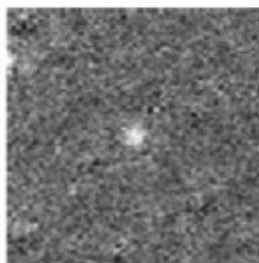
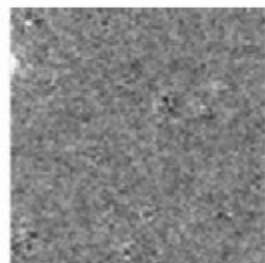
OA UW – prof. Andrzej Udalski  
warszawski teleskop w Chile  
Las Campanas



Gdy źródło przekracza  
pierścień Einsteina pojawiają  
się 2 obrazy  
\* odległe o ok. 1 mas  
nie sposób ich zobaczyć oddzielnie  
widzimy 1 obraz źródła, lecz  
jaśniejszy niż bez soczewkowania  
\* ruch względny soczewki i źródła  
przejawia się zmianą jasności  
źródła w czasie

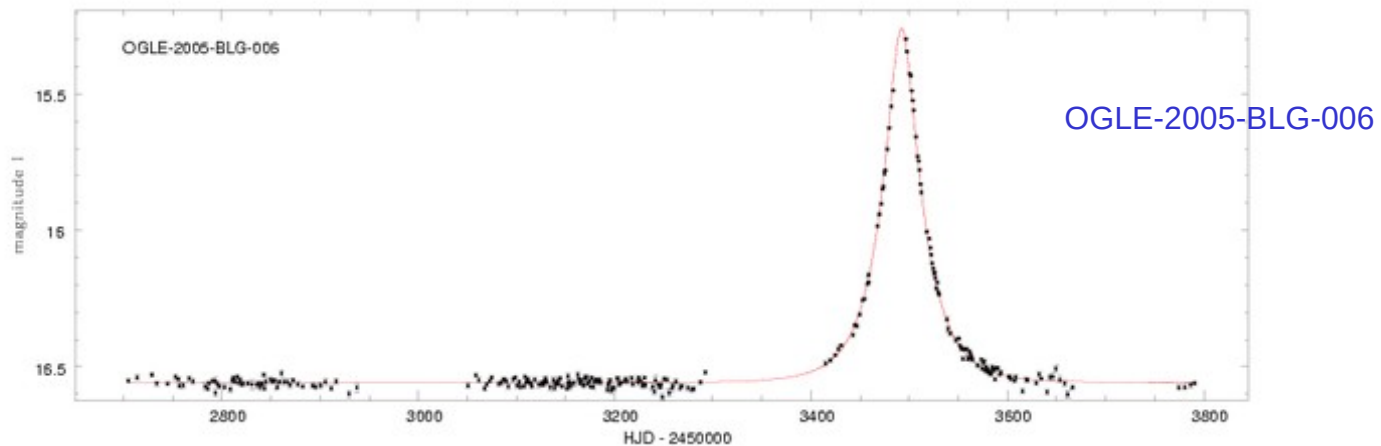
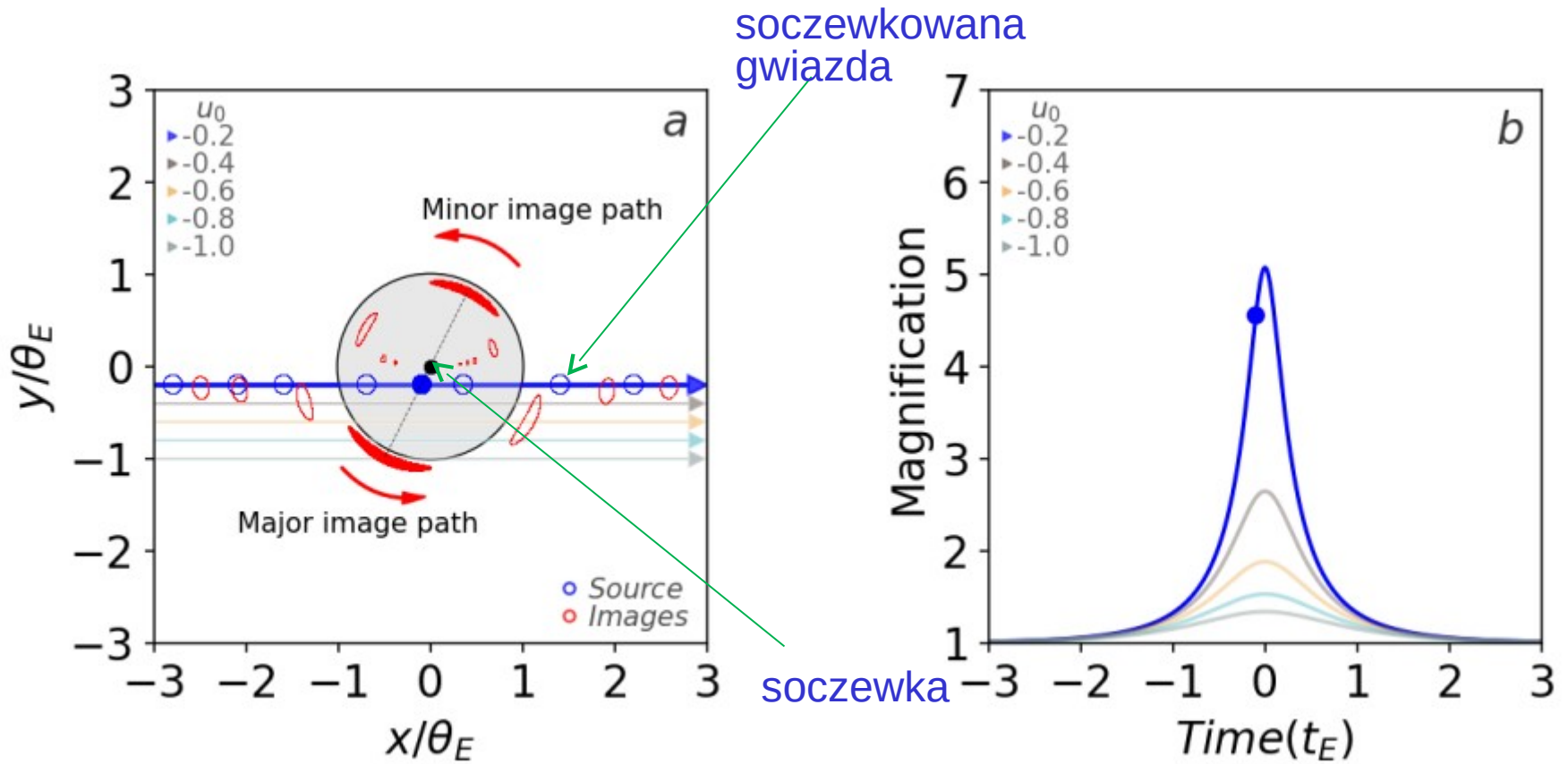


Observations



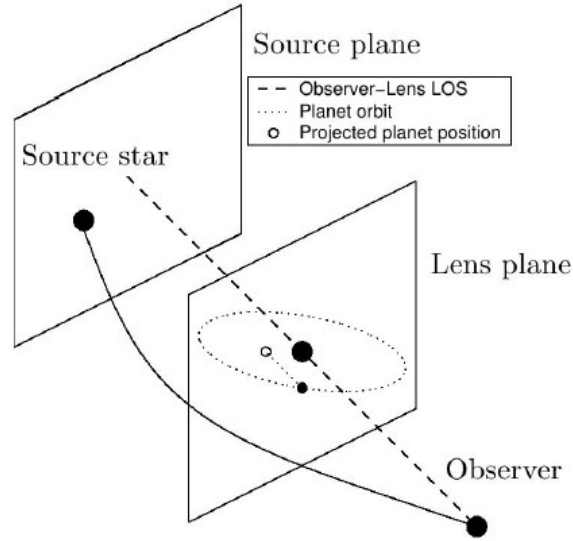
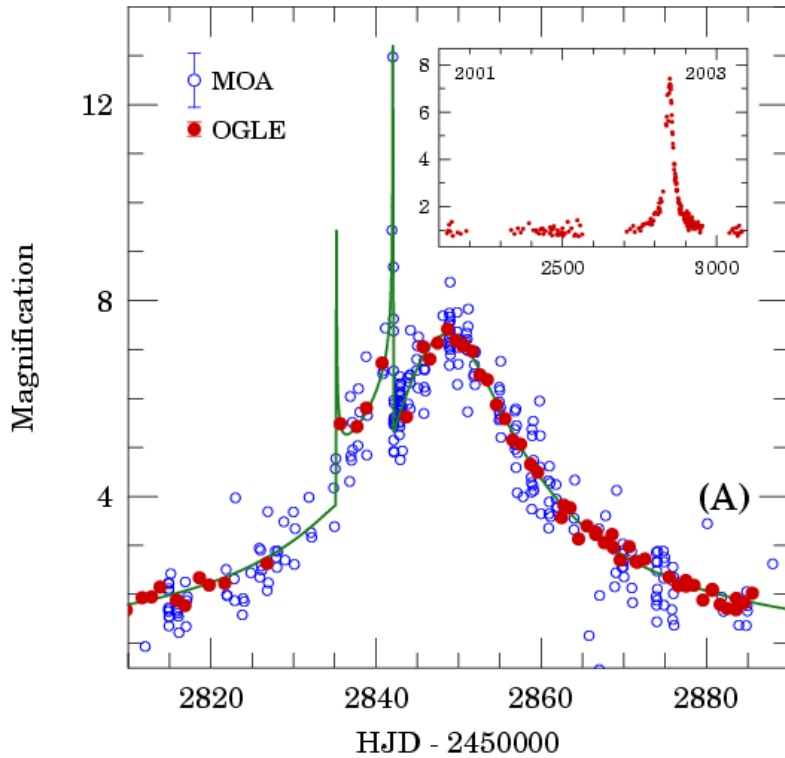
Difference Images

# Krzywa blasku w zjawisku mikrosoczewkowania

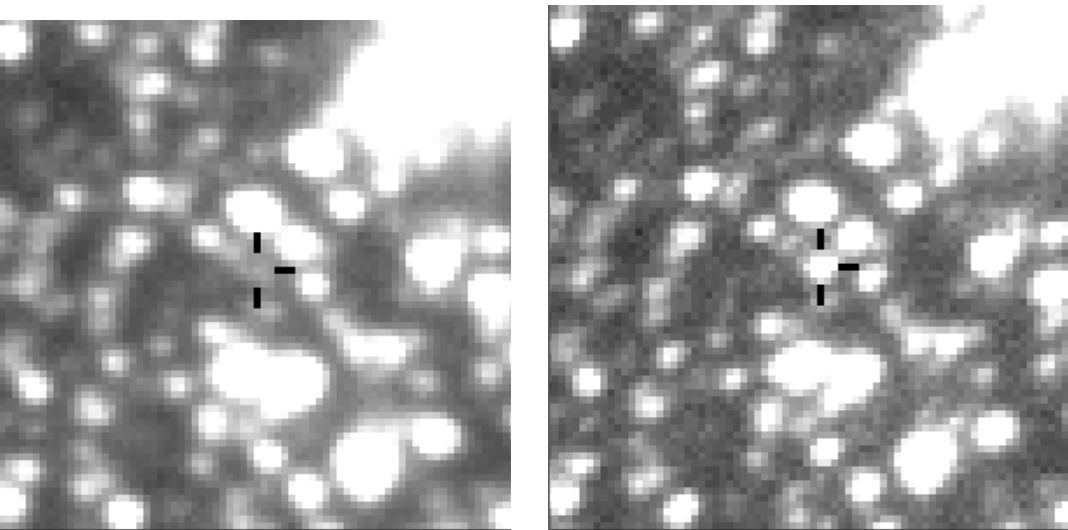




# Poszukiwania planet pozasłonecznych – B.Paczyński, Shude Mao 1991



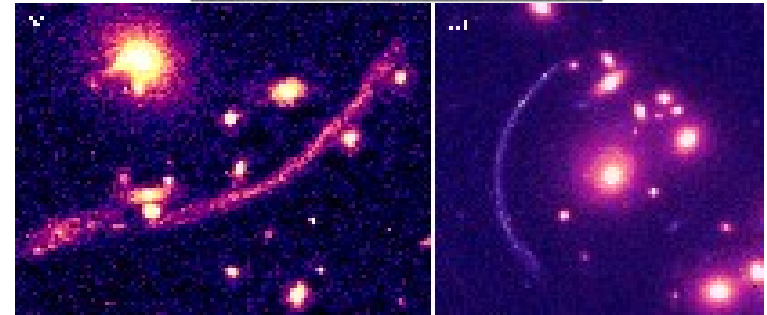
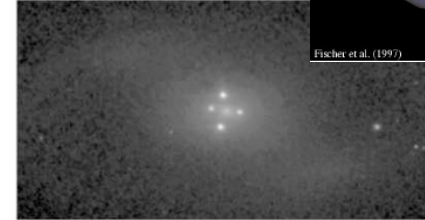
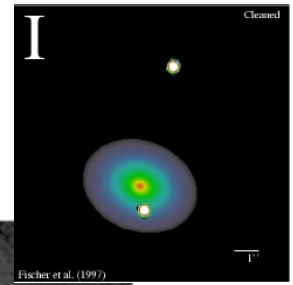
Obecnie prof. w Tshinghua U.  
+ Manchester U. (Jodrell Bank)



tą techniką odkryto już  
19 pozasłonecznych  
układów planetarnych

# Soczewkowanie grawitacyjne

- Refsdal 1964 pomiary  $H_0$  z soczewkowania
- Walsh, Carswell & Weymann 1979 - QSO-0957+561A,B
- „tajemnicze” olbrzymie łuki w gromadach w gromadach A370, Cl2244 (Paczyński sugeruje soczewkowanie)  
Soucail, Fort, Mellier 1987 potwierdzają to spektroskopowo
- w okresie 1978 – 1992 odkryto 11 soczewek
- w 2006 znano ich ok. 70
- obecnie ponad **300** soczewek: bieżące przeglądy SLACS, BELLS, CFHT – SL2S, CLASS, SQLS, HAGGLEs, AEGIS, COSMOS, CASSOWARY
- w przyszłości Pan-STARRS, **LSST**, JDES, SKA dostarczą **tysiący** nowych silnie soczewkowanych układów

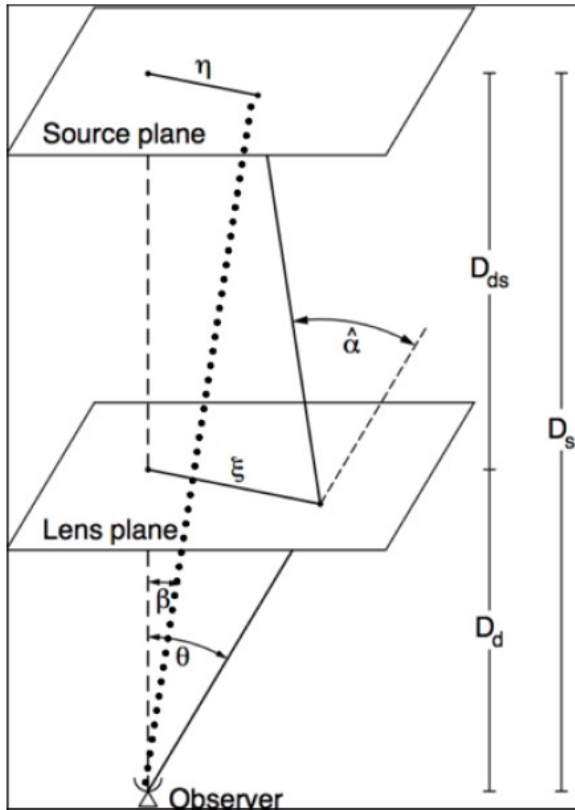




# Soczewkowanie grawitacyjne



## Formalizm promieni świetlnych

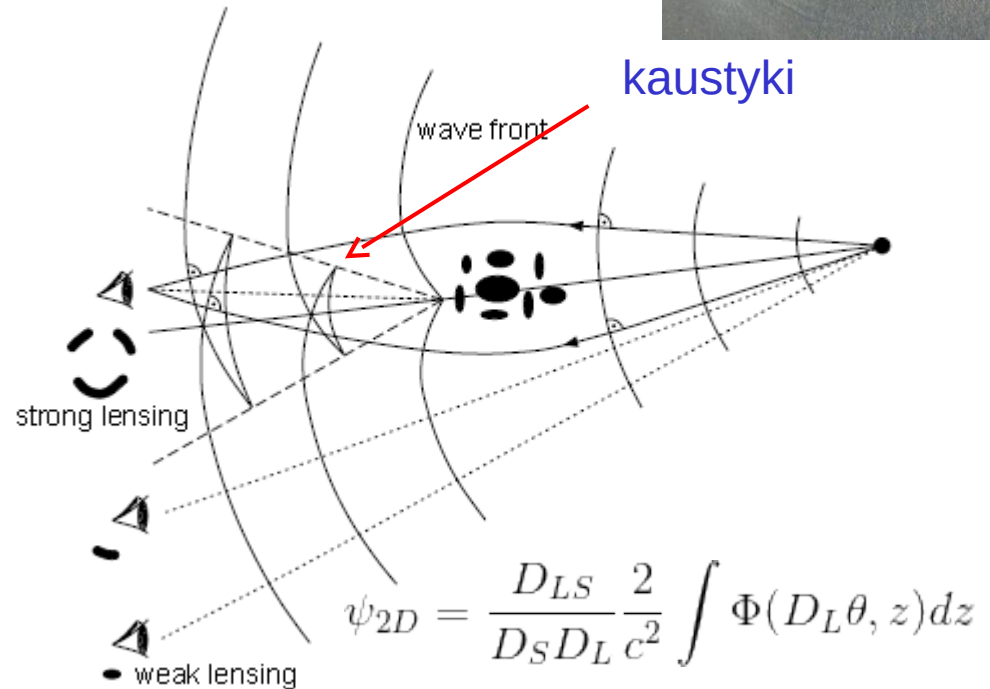


$$\hat{\alpha}(\theta) D_{ls} + \beta D_s = \theta D_s$$

$$\beta = \theta - \hat{\alpha}(\theta)$$

gradient  $\psi_{2D}$   $\uparrow$

## Formalizm frontów falowych (zasada Fermata)



$$\psi_{2D} = \frac{D_{LS}}{D_S D_L} \frac{2}{c^2} \int \Phi(D_L \theta, z) dz$$

## Czas przelotu

$$\tau = \frac{1 + z_L}{c} \frac{D_L D_S}{D_{LS}} \left[ \frac{1}{2} (\vec{\theta} - \vec{\beta})^2 - \psi_{2D}(\vec{\theta}) \right]$$

$$\nabla \tau(\theta; \beta) = 0.$$

Człon geometryczny  $\uparrow$

efekt Shapiro  $\uparrow$

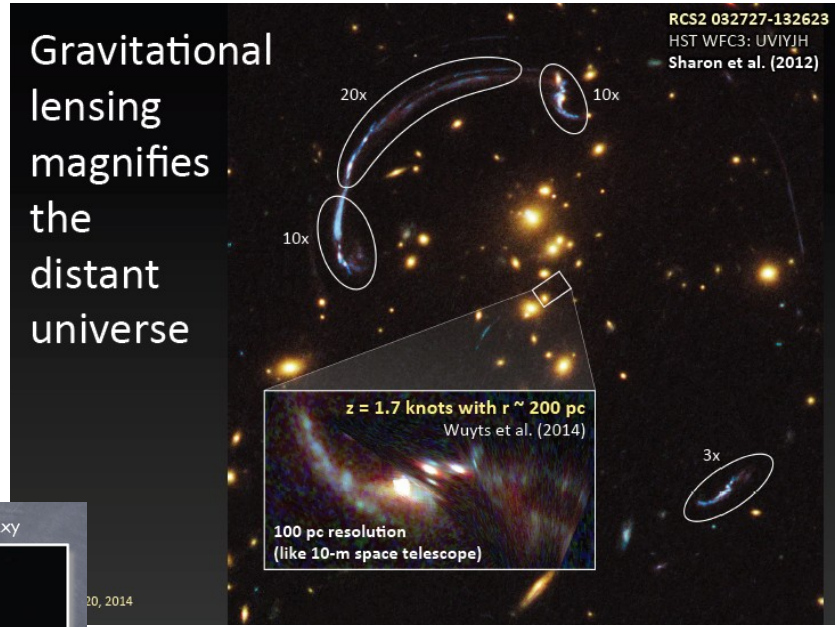
$$\vec{\theta} - \vec{\beta} - \frac{\partial \psi_{2D}}{\partial \vec{\theta}} = 0$$

Równanie soczewki

# Zastosowania silnego soczewkowania

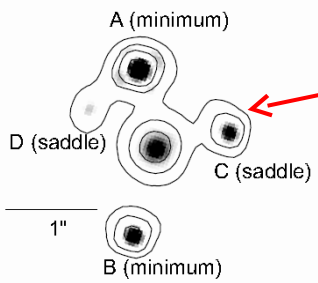
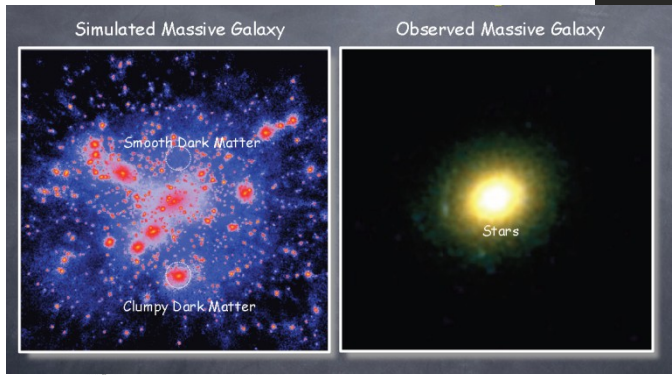
Badanie struktury galaktyk w różnych stadiach ewolucji:  
 soczewkowanie + kinematyka gwiazd  
 soczewki jako „kosmiczne teleskopy”

Badania ciemnej materii w skali galaktyk:  
 „brakujące” skupiska masy na małych skalach:  
 anomalne jasności makroobrazów  
 mikrosoczewkowanie



Różnice jasności makro-obrazów;

Teoria podpowiada sekwencję jasności

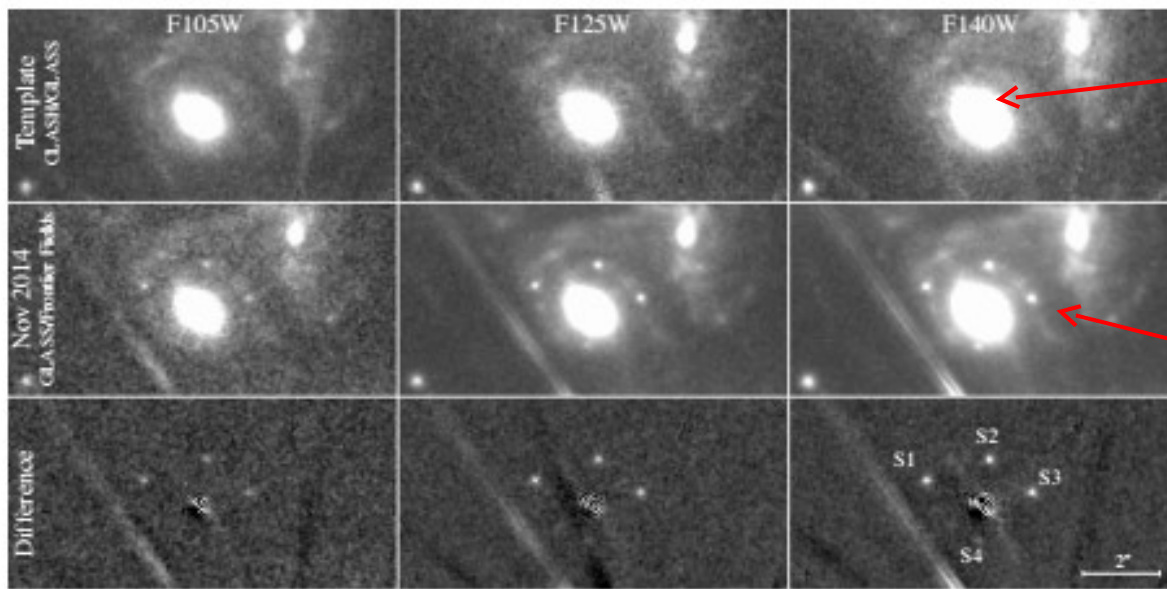


Anomalie jasności

Efekt soczewkowania przez zagęszczenia ciemnej materii (?)

# Supernowa „Refsdala”

Supernowa „Refsdala” odkryta 11 listopada 2014  
Kelly et al. (2015) *Science* 347, 1123



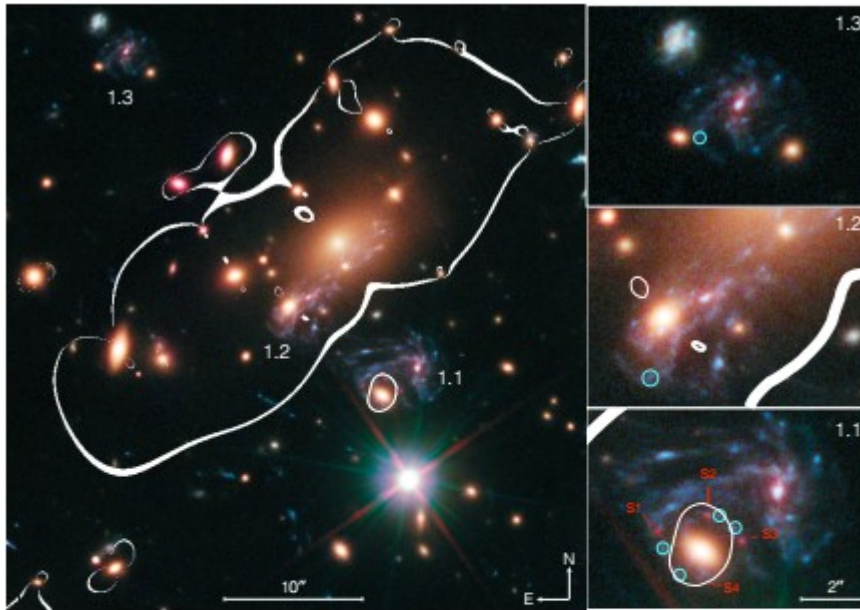
galaktyka eliptyczna  $z=0.54$   
należąca do gromady  
MACS J1149.6+2223

galaktyka spiralna  $z=1.49$   
źródło

galaktyka macierzysta SNI

**Fig. 1:** *HST* WFC3-IR images showing the simultaneous appearance of four point sources around a cluster member galaxy. From left to right the columns show imaging in the *F105W* filter (*Y* band), *F125W* (*J*), and *F140W* (*JH*). From top to bottom the

# Supernowa „Refsdala”



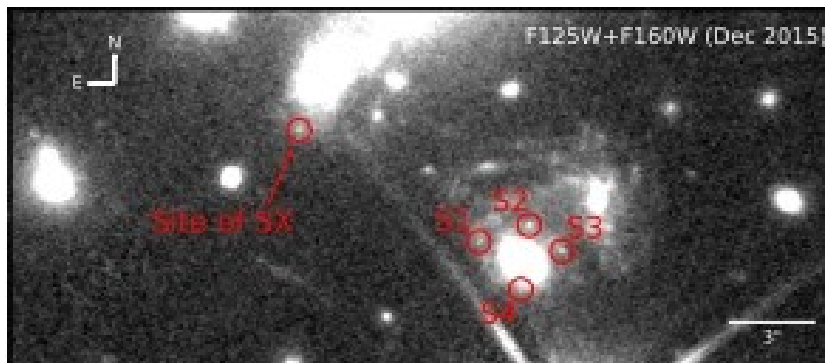
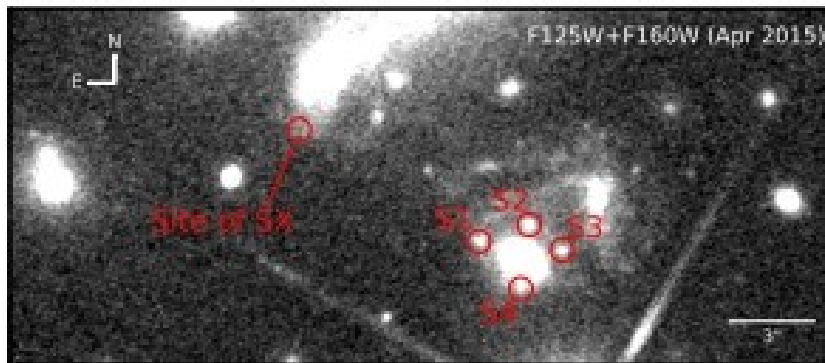
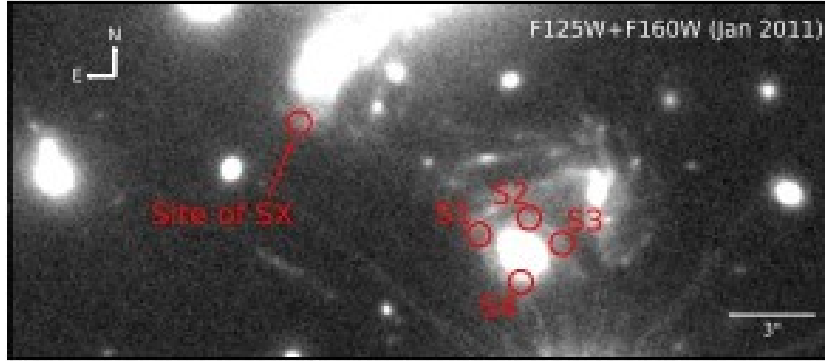
Powtórne pojawienie się przewidziane za ok. 1 rok

W jednym z obrazów galaktyki macierzystej soczewkowanej przez gromadę

**Fig. 2:** Color-composite image of the galaxy cluster MACSJ1149.6+2223, with critical curves for sources at the  $z = 1.49$  redshift of the host galaxy overlaid. Three images of the host galaxy formed by the cluster are marked with white labels (1.1, 1.2, and 1.3) in the left panel, and each is enlarged at right. The four current images of SN Refsdal that we detected (labeled S1 to S4 in red) appear as red point sources in image 1.1. Our model indicates that an image of the SN appeared in the past in image 1.3, and that one will appear in the near future in image 1.2. The extreme red hue of the SN may be somewhat exaggerated, because the blue and green channels include only data taken before the SN erupted. In image 1.1, both a single bright blue knot (cyan circles) and SN Refsdal are multiply imaged into four distinct locations. The image combines infrared and optical *HST* imaging data from the Frontier Fields and GLASS programs, along with images from the CLASH and the FrontierSN programs (GO-13790, PI: S.A.R.).



# Supernowa „Refsdala”



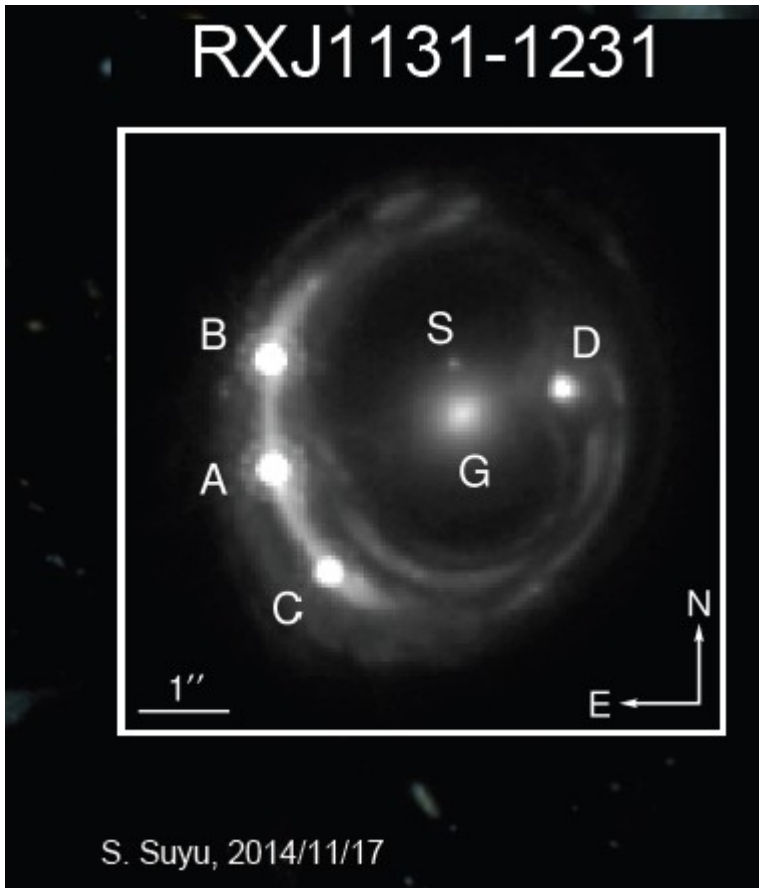
Kelly et al. (2016) ApJL

11 grudnia 2015  
SNII zaobserwowana  
w obrazie SX –  
zgodnie z przewidywaniami

**Wielki sukces astrofizyki**  
(OTW + teoria soczewkowania  
+ modelowanie rozkładu  
masy)

Porównywalny z triumfem  
mechaniki niebieskiej w XIX w.  
przy odkryciu Neptuna

# Metoda opóźnień czasowych w Kosmologii

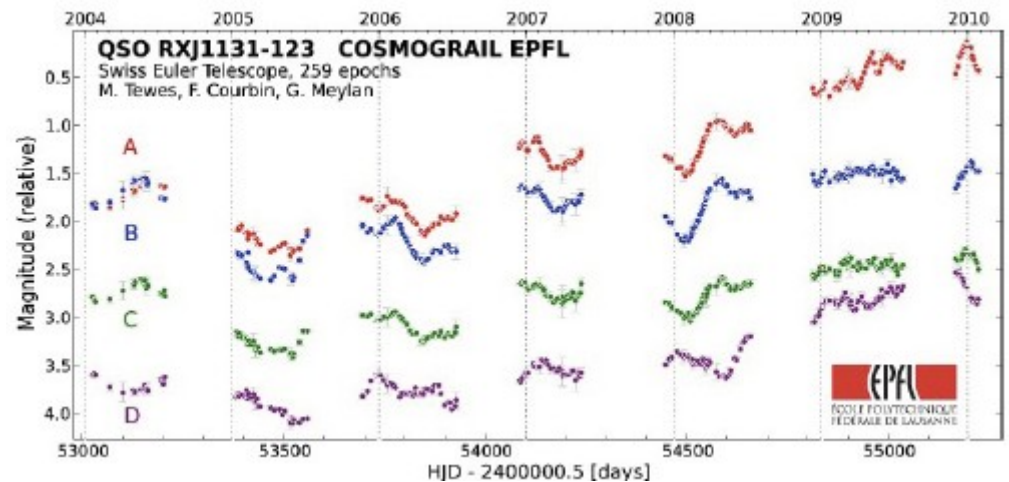


Results: Suyu et al. 2013

$$t(\vec{\theta}) = \frac{(1+z_d)}{c} \frac{D_d D_s}{D_{ds}} \left[ \frac{1}{2} (\vec{\theta} - \vec{\beta})^2 - \psi(\vec{\theta}) \right]$$

Time delay distance (points to  $\frac{D_d D_s}{D_{ds}}$ )  
Shapiro delay (points to  $-\psi(\vec{\theta})$ )  
Excess time delay (points to  $t(\vec{\theta})$ )  
geometric time delay (points to  $\frac{1}{2} (\vec{\theta} - \vec{\beta})^2$ )

Opóźnienie czasowe – największa osiągalna dokładność 1.5%

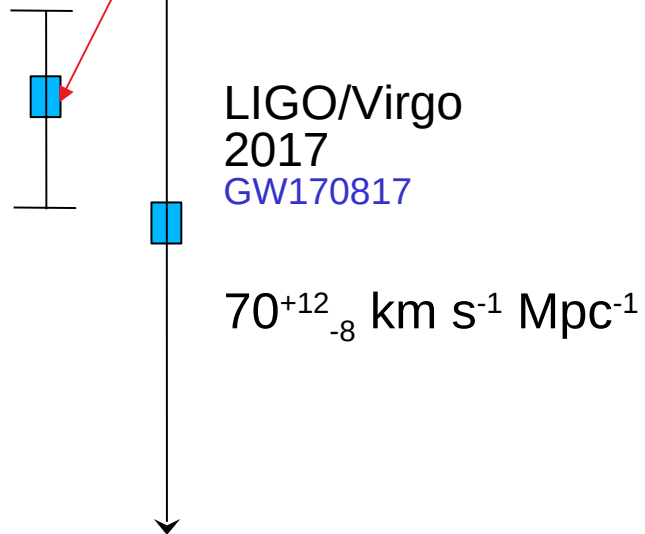
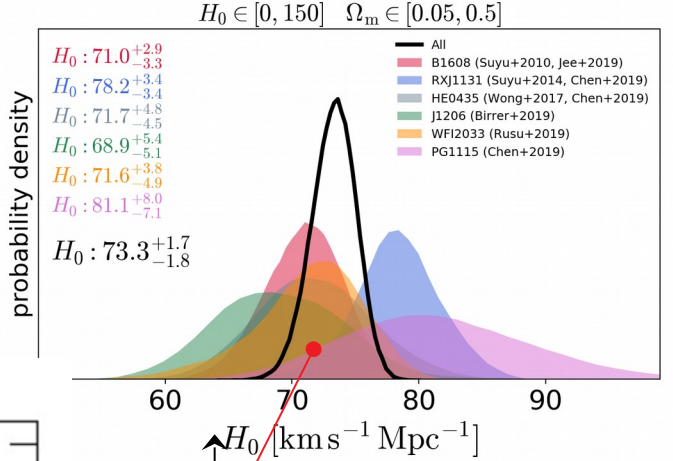
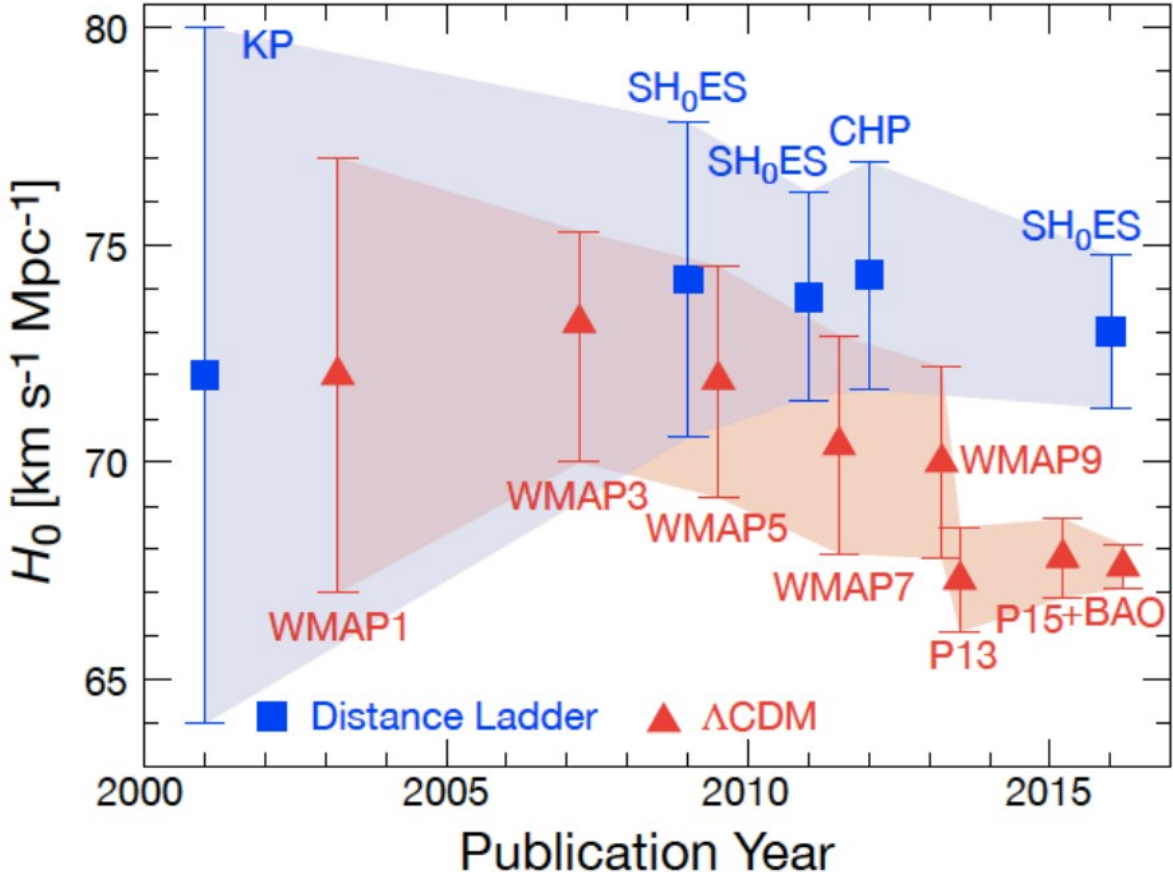


$$H_0 = 73.3^{+1.7}_{-1.8} \text{ km s}^{-1} \text{ Mpc}^{-1}$$



# H0LiCOW XIII. A 2.4% measurement of $H_0$ from lensed quasars: $5.3\sigma$ tension between early and late-Universe probes

Kenneth C. Wong,<sup>1,2\*</sup> Sherry H. Suyu,<sup>3,4,5</sup> Geoff C.-F. Chen,<sup>6</sup> Cristian E. Rusu,<sup>2,7,6</sup> Martin Millon,<sup>8</sup> Dominique Sluse,<sup>9</sup> Vivien Bonvin,<sup>8</sup> Christopher D. Fassnacht,<sup>6</sup> Stefan Taubenberger,<sup>3</sup> Matthew W. Auger,<sup>10</sup> Simon Birrer,<sup>11</sup> James H. H. Chan,<sup>8</sup> Frederic Courbin,<sup>8</sup> Stefan Hilbert,<sup>12,13</sup> Olga Tihhonova,<sup>8</sup> Tommaso Treu,<sup>11</sup> Adriano Agnello,<sup>14</sup> Xuheng Ding,<sup>11</sup> Inh Jee,<sup>3</sup> Eiichiro Komatsu,<sup>3,1</sup> Anowar J. Shahjib,<sup>11</sup> Alessandro Sonnenfeld,<sup>15</sup> Roger D. Blandford,<sup>16</sup> Léon V. E. Koopmans,<sup>17</sup> Philip J. Marshall,<sup>16</sup> and Georges Meylan<sup>8</sup>



# Zagadką jest przyspieszające tempo ekspansji Wszechświata

Znane jako „problem ciemnej energii”

Równania Einsteina przewidują, że tempo ekspansji powinno spowalniać (jeśli Wszechświat byłby wypełniony zwykłą materią), natomiast widzimy, że przyspiesza ...

Co jest za to odpowiedzialne?



Nagroda Nobla z Fizyki 2011

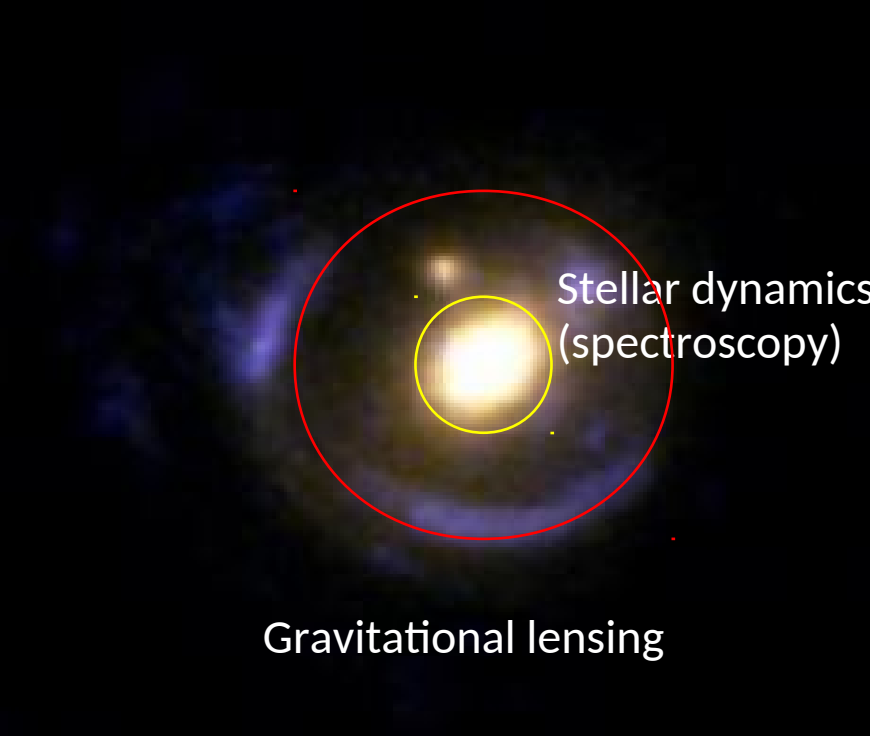


## Pytania fizyki fundamentalnej

Czy ogólna teoria względności jest właściwą teorią grawitacji ?

Czy stałe fundamentalne mogą mieć naturę dynamiczną ?

Czy można testować kwantową teorię grawitacji ?



Pomysł dyspersja prędkości – spektroskopia

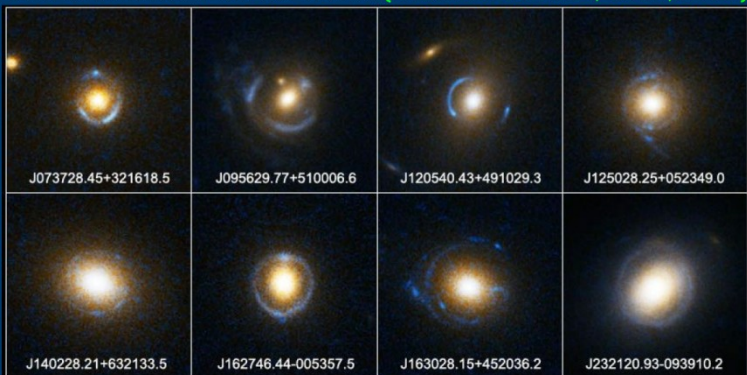
$$\theta_E = 4 \pi \left( \frac{\sigma_v}{c} \right)^2 \frac{D_{LS}}{D_S}$$

z astrometrii obrazów

Iloraz odległości zależy od modelu kosmologicznego

## Sloan Lens ACS (SLACS) Survey

HST (Snapshot) Survey of spectroscopically selected lens-candidates from the SDSS. (Bolton et al. 2004, 2005, 2006)



Monthly Notices

of the  
ROYAL ASTRONOMICAL SOCIETY

Mon. Not. R. Astron. Soc. **406**, 1055–1059 (2010)

doi:10.1111/j.1365-2966.2010.16725.x

## Cosmic equation of state from strong gravitational lensing systems

Marek Biesiada,<sup>\*</sup> Aleksandra Piórkowska<sup>\*</sup> and Beata Malec<sup>\*</sup>

Department of Astrophysics and Cosmology, Institute of Physics, University of Silesia, Uniwersytecka 4, 40-007 Katowice, Poland

Constraints on cosmological models from strong gravitational lensing systems

Shuo Cao,<sup>a</sup> Yu Pan,<sup>a,b</sup> Marek Biesiada,<sup>c</sup> Włodzimierz Godłowski<sup>d</sup> and Zong-Hong Zhu<sup>a,1</sup>

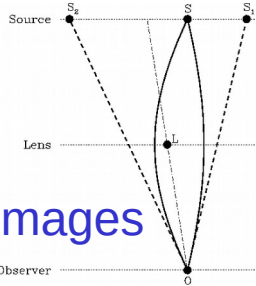
JCAP03 (2012) 016

10 gromad w roli soczewek  
70 galaktyk w roli soczewek z przeglądu SLACS

Próbka układów z 2 obrazami

36 SLACS lenses

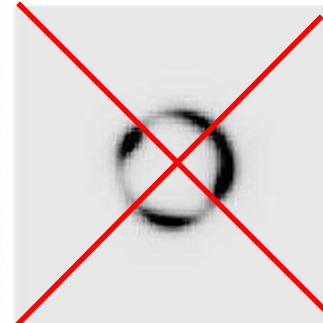
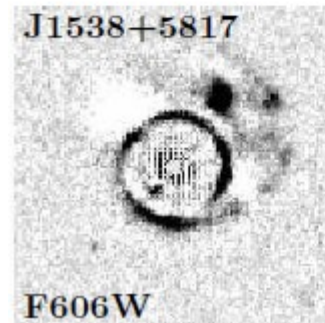
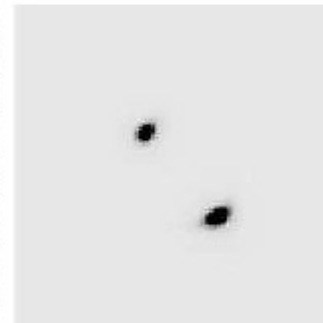
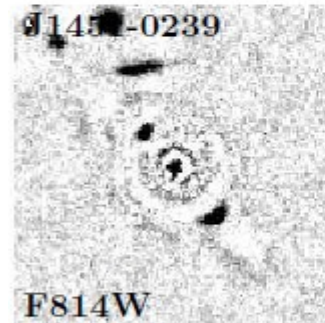
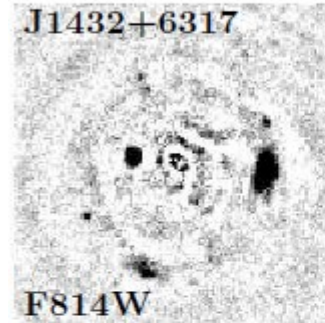
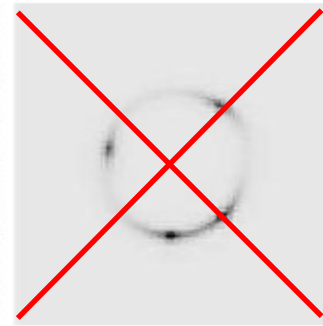
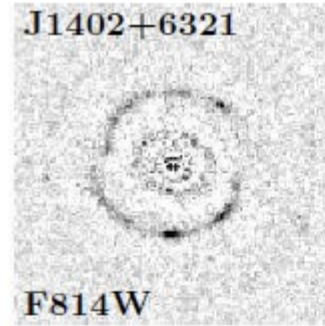
Marginalizacja po  $f_E$



$$\theta_E = 4\pi \frac{\sigma_{SIS}^2}{c^2} \frac{D_{ls}}{D_s}$$

$$\sigma_{SIS} = f_E \sigma_0$$

$$D^{obs} = \frac{c^2 \theta_E}{4\pi \sigma_0^2 f_E^2}$$



2 images

| Cosmological model | Best-fitting parameters ( $n = 80$ )            | Best-fitting parameters ( $n = 46$ )             |
|--------------------|---|--|
| $\Lambda$ CDM      | $\Omega_m = 0.20^{+0.07}_{-0.07}$               | $\Omega_m = 0.26^{+0.11}_{-0.10}$                |
| wCDM               | $w = -1.02^{+0.26}_{-0.26}$                     | $w = -1.15^{+0.34}_{-0.35}$                      |
| CPL                | $w_0 = 0.60 \pm 1.76$<br>$w_a = -7.37 \pm 8.05$ | $w_0 = -0.24 \pm 2.42$<br>$w_a = -6.35 \pm 9.75$ |

WMAP7+BAO+H0

$\Omega_m = 0.272$   
 $w = -1.10 \pm 0.14$   
 $w_0 = -0.93 \pm 0.13$   
 $w_a = -0.41 \pm 0.71$   
 Komatsu et al. 2011



## COSMOLOGY WITH STRONG-LENSING SYSTEMS

SHUO CAO<sup>1</sup>, MAREK BIESIADA<sup>1,2</sup>, RAPHAËL GAVAZZI<sup>3</sup>, ALEKSANDRA PIÓRKOWSKA<sup>2</sup>, AND ZONG-HONG ZHU<sup>1</sup>

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<sup>2</sup>Department of Astrophysics and Cosmology, Institute of Physics, University of Silesia, Uniwersytecka 4, 40-007, Katowice, Poland

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Received 2015 January 23; accepted 2015 May 1; published 2015 June 17

### Sferycznie symetryczny potęgowy profil rozkładu masy

$$\rho \propto r^{-\gamma}$$

**Soczewkowanie:** masa wewnątrz promienia Einsteina

$$M_{\text{lens}} = \frac{c^2}{4G} \frac{D_s D_l}{D_{ls}} \theta_E^2$$



$$M_{\text{dyn}} = \frac{\pi}{G} \sigma_{\text{ap}}^2 R_E \left( \frac{R_E}{R_{\text{ap}}} \right)^{2-\gamma} f(\gamma)$$

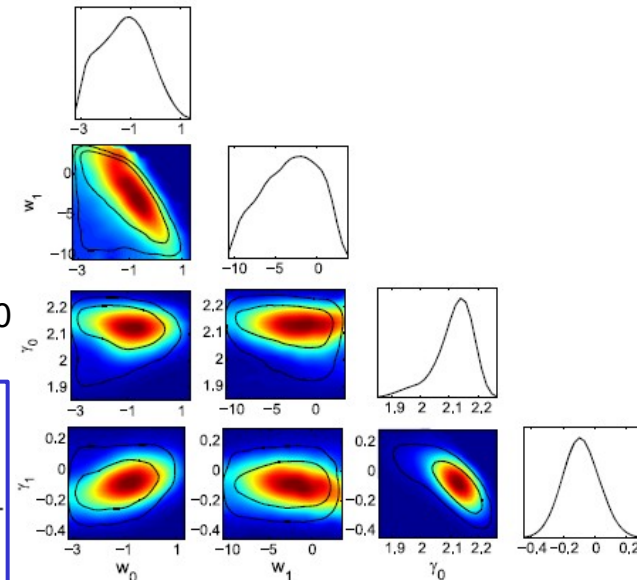
$$= \frac{\pi}{G} \sigma_{\text{ap}}^2 D_l \theta_E \left( \frac{\theta_E}{\theta_{\text{ap}}} \right)^{2-\gamma} f(\gamma)$$

$$\gamma(z_l) = \gamma_0 + \gamma_1 z_l$$

ewolucja  $\gamma$

A. Ruff, R. Gavazzi et al. 2010

118 soczewek z przeglądu SLACS



$$\theta_E = 4\pi \frac{\sigma_{\text{ap}}^2}{c^2} \frac{D_{ls}}{D_s} \left( \frac{\theta_E}{\theta_{\text{ap}}} \right)^{2-\gamma} f(\gamma)$$

$$D^{\text{obs}} = \frac{c^2 \theta_E}{4\pi \sigma_{\text{ap}}^2} \left( \frac{\theta_{\text{ap}}}{\theta_E} \right)^{2-\gamma} f^{-1}(\gamma)$$

vs.

$$D^{\text{th}}(z_l, z_s; p) = \frac{D_{ls}(p)}{D_s(p)} = \frac{\int_{z_l}^{z_s} \frac{dz'}{h(z'; p)}}{\int_0^{z_s} \frac{dz'}{h(z'; p)}}$$



# TEST OF PARAMETRIZED POST-NEWTONIAN GRAVITY WITH GALAXY-SCALE STRONG LENSING SYSTEMS

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<sup>1</sup>Department of Astronomy, Beijing Normal University, 100875, Beijing, China; zhuzh@bnu.edu.cn

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Received 2016 September 11; revised 2016 November 18; accepted 2016 December 2; published 2017 January 20

THE ASTROPHYSICAL JOURNAL, 835:92 (7pp), 2017 January 20

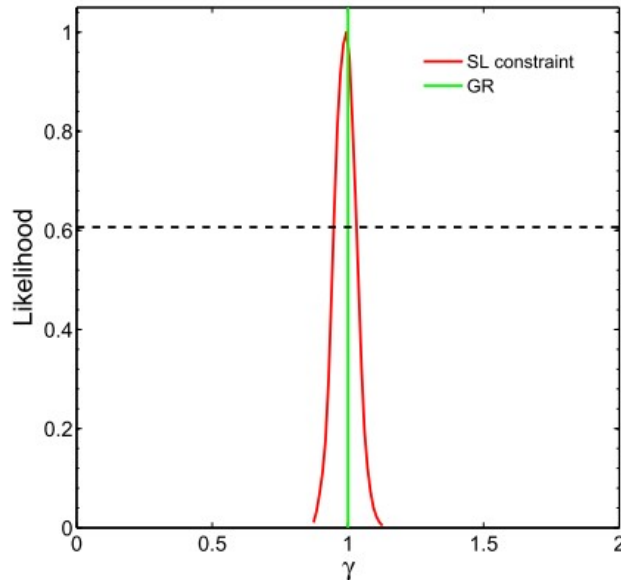


Figure 3. Normalized posterior likelihood of the PPN  $\gamma$  parameter obtained with rigid priors on the nuisance parameters ( $\alpha$ ,  $\beta$ ,  $\delta$ ).

$$\gamma = 0.995^{+0.037}_{-0.047}$$

How much space curvature  $g_{ij}$  is produced by unit rest mass ?

Table 1

Sensitivity of Constraints on  $\gamma$  with Respect to the Galaxy Structure Parameters

| Systematics                                  | PPN Parameter                      |
|--|------------------------------------|
| $\alpha = 2.00; \beta = 0.18; \delta = 2.40$ | $\gamma = 0.995^{+0.037}_{-0.047}$ |
| $\alpha = 1.92; \beta = 0.18; \delta = 2.40$ | $\gamma = 0.860 \pm 0.040$         |
| $\alpha = 2.08; \beta = 0.18; \delta = 2.40$ | $\gamma = 1.169 \pm 0.050$         |
| $\alpha = 2.00; \beta = 0.05; \delta = 2.40$ | $\gamma = 0.914 \pm 0.043$         |
| $\alpha = 2.00; \beta = 0.31; \delta = 2.40$ | $\gamma = 1.087 \pm 0.043$         |
| $\alpha = 2.00; \beta = 0.18; \delta = 2.29$ | $\gamma = 1.111 \pm 0.044$         |
| $\alpha = 2.00; \beta = 0.18; \delta = 2.51$ | $\gamma = 0.883 \pm 0.039$         |

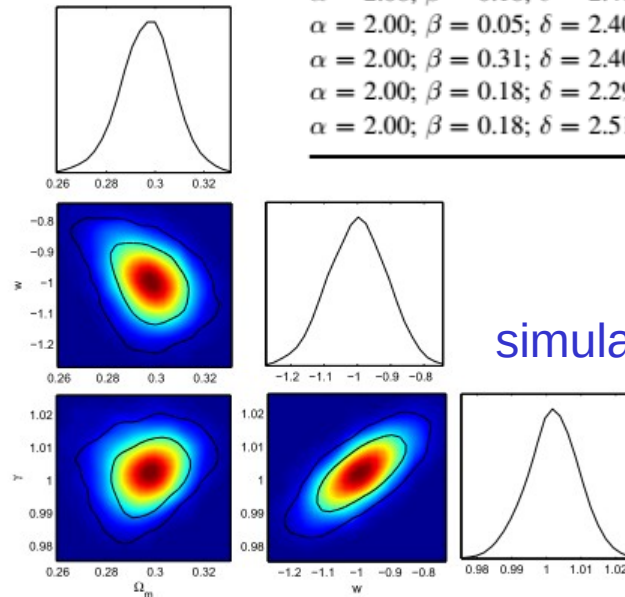


Figure 7. Constraints on the PPN parameter and cosmological parameters from the simulated LSST strong lensing data.





# Testing the Speed of Light over Cosmological Distances: The Combination of Strongly Lensed and Unlensed Type Ia Supernovae

Shuo Cao<sup>1</sup> , Jingzhao Qi<sup>1</sup>, Marek Biesiada<sup>1,2</sup> , Xiaogang Zheng<sup>1</sup>, Tengteng Xu<sup>1</sup>, and Zong-Hong Zhu<sup>1</sup> 

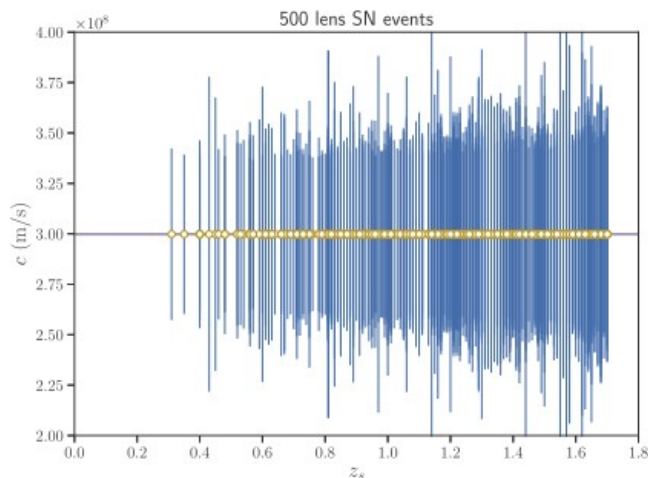
<sup>1</sup>Department of Astronomy, Beijing Normal University, Beijing 100875, People's Republic of China; [zhuzh@bnu.edu.cn](mailto:zhuzh@bnu.edu.cn)

<sup>2</sup>Department of Astrophysics and Cosmology, Institute of Physics, University of Silesia, 75 Pułku Piechoty 1, 41-500 Chorzów, Poland; [marek.biesiada@us.edu.pl](mailto:marek.biesiada@us.edu.pl)

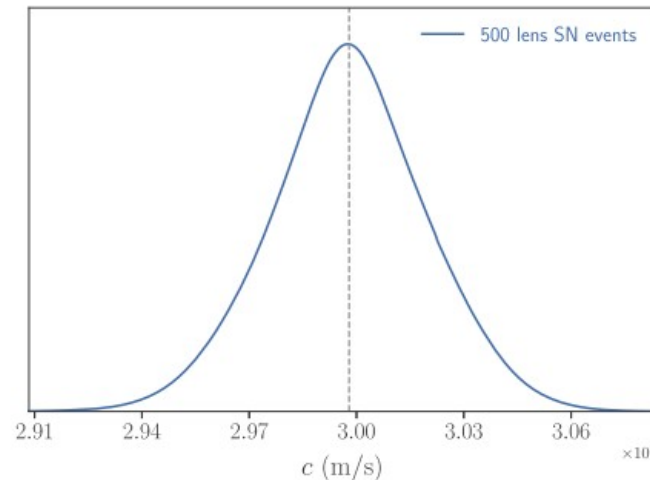
Received 2018 August 4; revised 2018 September 23; accepted 2018 October 1; published 2018 October 30

## Abstract

Probing the speed of light is an important test of general relativity, but the measurements of  $c$  using objects in the distant universe have been almost completely unexplored. In this paper, we propose an idea to use the multiple measurements of galactic-scale strong gravitational lensing systems with Type Ia supernovae acting as background sources to estimate the speed of light. This provides an original method to measure the speed of light using objects located at different redshifts that emitted their light in a distant past. Moreover, we predict that strongly lensed Type Ia supernovae observed by the Large Synoptic Survey Telescope (LSST) would produce robust constraints on  $\Delta c/c$  at the level of  $10^{-3}$ . We also discuss whether future surveys such as LSST may succeed in detecting any hypothetical variation of  $c$  predicted by theories in which fundamental constants have a dynamical nature.



**Figure 1.** Individual measurements of the speed of light from the forthcoming LSST survey.



**Figure 2.** Probability distribution of the speed of light  $c$  possible to obtain from the forthcoming LSST survey.

$$\frac{\Delta c}{c} = 0.005$$

### Strongly gravitationally lensed type Ia supernovae: Direct test of the Friedman-Lemaître-Robertson-Walker metric

Jingzhao Qi,<sup>1,2</sup> Shuo Cao,<sup>2,\*</sup> Marek Biesiada,<sup>2,3</sup> Xiaogang Zheng,<sup>4</sup> Xuheng Ding,<sup>4</sup> and Zong-Hong Zhu<sup>2,4,†</sup>

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 (Received 13 October 2018; published 19 July 2019)

We present a new idea of testing the validity of the Friedman-Lemaître-Robertson-Walker (FLRW) metric, through the multiple measurements of galactic-scale strong gravitational lensing systems with type Ia supernovae in the role of sources. Each individual lensing system will provide a model-independent measurement of the spatial curvature parameter referring only to geometrical optics independently of the matter content of the Universe. This will create a valuable opportunity to test the FLRW metric directly. Our results show that with hundreds of strongly lensed SNe Ia observed by the Large Synoptic Survey Telescope, one would produce robust constraints on the spatial curvature with accuracy  $\Delta\Omega_k = 0.04$  comparable to the *Planck* 2015 results.

PHYS. REV. D **100**, 023530 (2019)

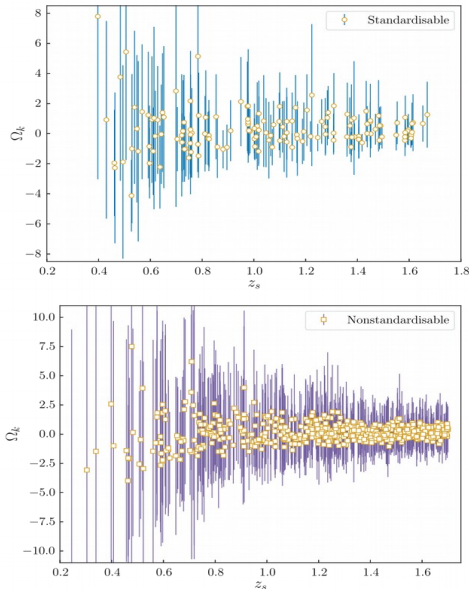


FIG. 1. An example of the simulated measurements of  $\Omega_k$  from future observations of SGLSNe Ia: without and with the effect of microlensing. The blue lines denote the associated error bars (68.3% C.L.) of  $\Omega_k$  when all the uncertainties are included.

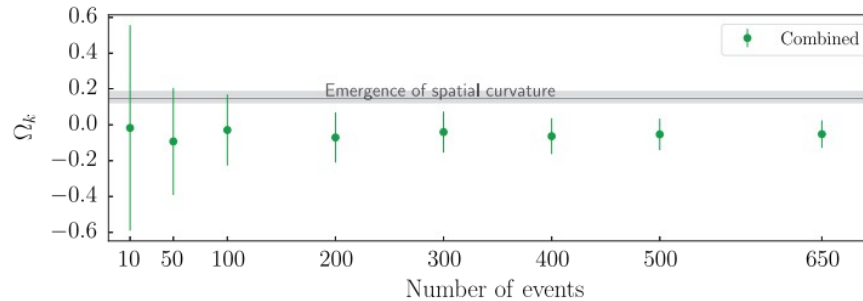
## Możliwość wyznaczenia krzywizny Wszechświata z soczewkowanych SN Ia

$$\frac{d_{ls}}{d_s} = \sqrt{1 + \Omega_k d_l^2} - \frac{d_l}{d_s} \sqrt{1 + \Omega_k d_s^2}.$$

$$D_l = (1 + z_l) D_{\Delta t} \frac{D_{ls}^A}{D_s^A}.$$

$$D_s = \frac{10^{(\mu_D + 2.5 \log \mu)/5 - 5}}{1 + z_s} (\text{Mpc}).$$

$$\Omega_k(z_l, z_s) = \frac{d_l^4 + d_s^4 + d_{ls}^4 - 2d_l^2 d_s^2 - 2d_l^2 d_{ls}^2 - 2d_s^2 d_{ls}^2}{4d_l^2 d_s^2 d_{ls}^2}$$



650 soczewkowanych  
SN Ia z LSST

FIG. 3. Inferred  $\Omega_k$  parameter as a function of the number of SGLSNe Ia, with the prediction of a silent universe added for comparison.

## Perspektywy:

- Silnie soczewkowane układy o zmierzonych dyspersjach prędkości w galaktykach soczewkujących stanowią nową klasę "standardowych linijek"  
(promień Einstein wystandaryzowany przez kinematykę gwiazd)
- już dostarczyły pierwszych ocen parametrów kosmologicznych
- atrakcyjne z punktu widzenia degeneracji pomiędzy współczynnikami  $w_0$  i  $w_a$  w równaniu stanu „ciemnej energii”
- przy pomocy soczewek można wyznaczyć **krzywiznę przestrzeni !**
- z pewnością staną się techniką komplementarną do innych metod
- za pomocą soczewek będzie też można testować „**egzotyczną fizykę**”

# Fale grawitacyjne zarejestrowane dokładnie 100 lat po powstaniu OTW

## LIGO PRESS RELEASE

PRL 116, 061102 (2016)

Selected for a Viewpoint in *Physics*  
 PHYSICAL REVIEW LETTERS

week ending  
 12 FEBRUARY 2016



## Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott *et al.*\*

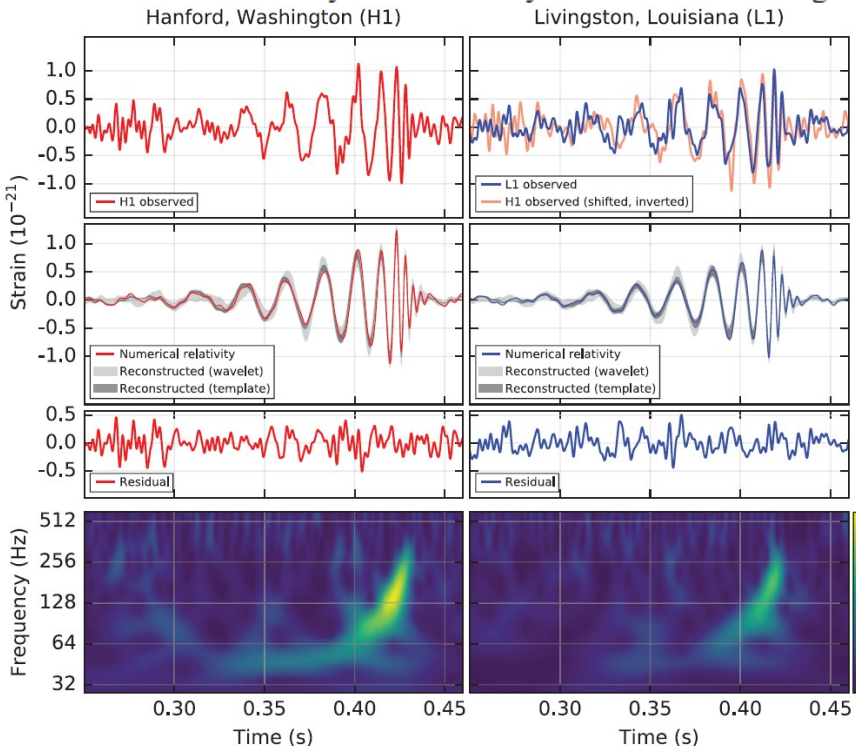
(LIGO Scientific Collaboration and Virgo Collaboration)

(Received 21 January 2016; published 11 February 2016)

On September 14, 2015 at 09:50:45 UTC the two detectors of the Laser Interferometer Gravitational-Wave Observatory simultaneously observed a transient gravitational-wave signal. The signal sw

e strain of  $1.0 \times 10^{-21}$ . It match  
 of a pair of black holes and the  
 matched-filter signal-to-noise r

LIGO opens new window on the universe with observation of gravitational waves from colliding black holes



Zarejestrowano

dotychczas 11  
 sygnałów  
 grawitacyjnych

- GW150914
- GW151012
- GW151226
- GW170104
- GW170608
- GW170814
- GW170817

+

- GW170729; GW170809
- GW170818
- GW170823



# Electromagnetic emission

Merger of NS-NS / NS-BH

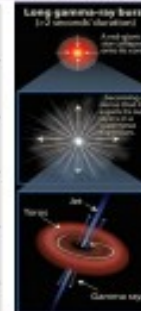
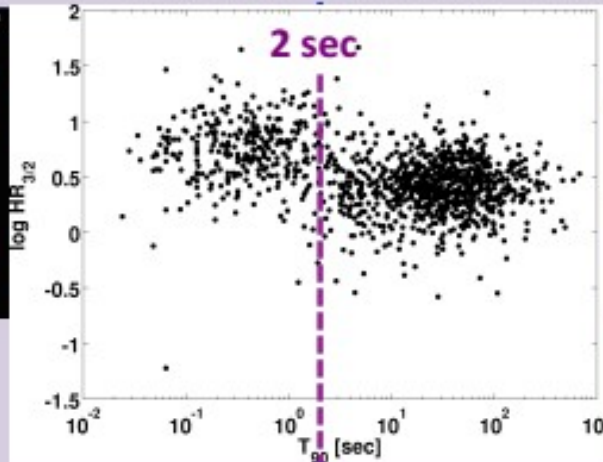
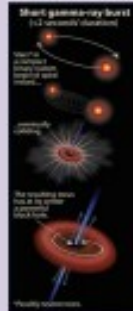
Core collapse of massive star

## Gamma-Ray Burst

### Short Hard GRB

Progenitor indications:

- lack of observed SN
- association with older stellar population
- larger distance from the host galaxy center (~ 5-10 kpc)



### Long Soft GRB

Progenitor strong evidence: observed Type Ic SN spectrum

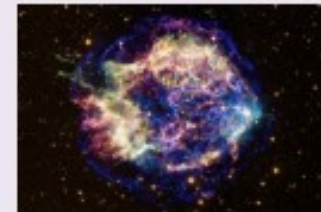
### Kilonovae

(Optical/IR, radio remnant)



### Supernovae

Type II, Ib/c



# Pierwszy model kilo-nowej (koalescencji dwóch gwiazd neutronowych)

ważny dla zrozumienia kosmicznej nukleosyntezy ...

THE ASTROPHYSICAL JOURNAL, 507:L59–L62, 1998 November 1  
© 1998. The American Astronomical Society. All rights reserved. Printed in U.S.A.

## TRANSIENT EVENTS FROM NEUTRON STAR MERGERS

LI-XIN LI AND BOHDAN PACZYŃSKI

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Received 1998 July 27; accepted 1998 August 26; published 1998 September 21

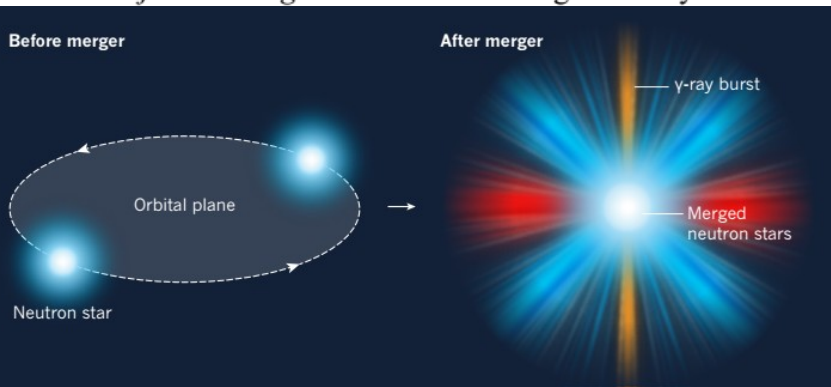
### ABSTRACT

Mergers of neutron stars (NS + NS) or neutron stars and stellar-mass black holes (NS + BH) eject a small fraction of matter with a subrelativistic velocity. Upon rapid decompression, nuclear-density medium condenses into neutron-rich nuclei, most of them radioactive. Radioactivity provides a long-term heat source for the expanding envelope. A brief transient has a peak luminosity in the supernova range, and the bulk of radiation in the UV-optical domain. We present a very crude model of the phenomenon, and simple analytical formulae that can be used to estimate the parameters of a transient as a function of poorly known input parameters. The mergers may be detected with high-redshift supernova searches as rapid transients, many of them far away from the parent galaxies. It is possible that the mysterious optical transients detected by Schmidt et al. are related to neutron star mergers, since they typically have no visible host galaxy.

*Subject headings:* binaries: close — gamma rays: bursts — stars: neutron — supernovae: general



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Obecnie prof. w Peking U.  
Kavli Institute of Astronomy  
and Astrophysics



# GW 170817 – Nowa era astronomii wielu nośników informacji (multimessenger astronomy)

PRL 119, 161101 (2017)

Selected for a Viewpoint in *Physics*  
PHYSICAL REVIEW LETTERS

week ending  
20 OCTOBER 2017



## GW170817: Observation of Gravitational Waves from a Binary Neutron Star Inspiral

B. P. Abbott *et al.*\*

(LIGO Scientific Collaboration and Virgo Collaboration)

(Received 26 September 2017; revised manuscript received 2 October 2017; published 16 October 2017)

17 sierpnia 2017 o godz. 12:41:04 UTC  
detektory LIGO/Virgo zarejestrowały  
pierwszy w historii sygnał grawitacyjny  
z koalescencji układu dwóch  
gwiazd neutronowych (NS-NS)

Odpowiadający temu zdarzeniu sygnał  
elektromagnetyczny został zarejestrowany  
• w promieniach gamma 1.7 s po koalescencji

(Fermi Gamma-ray  
Space Telescope  
NASA, INTEGRAL, Agile)

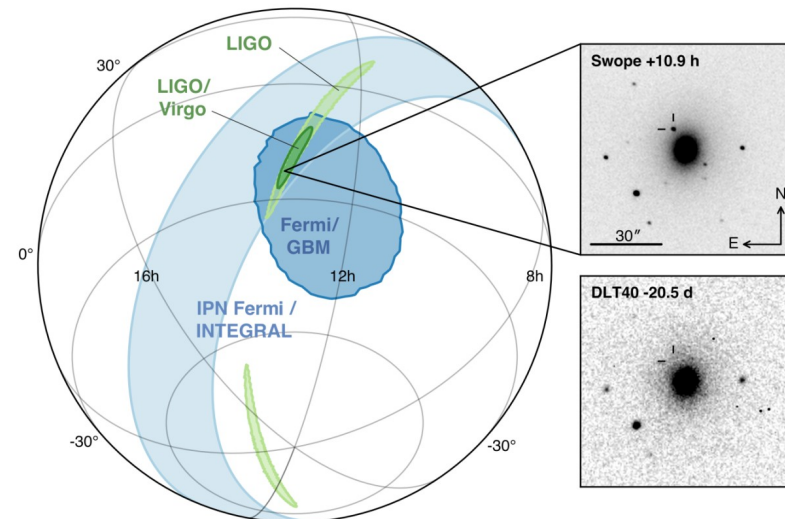
• w promieniach rentgena

(Swift, Magic, Integral)

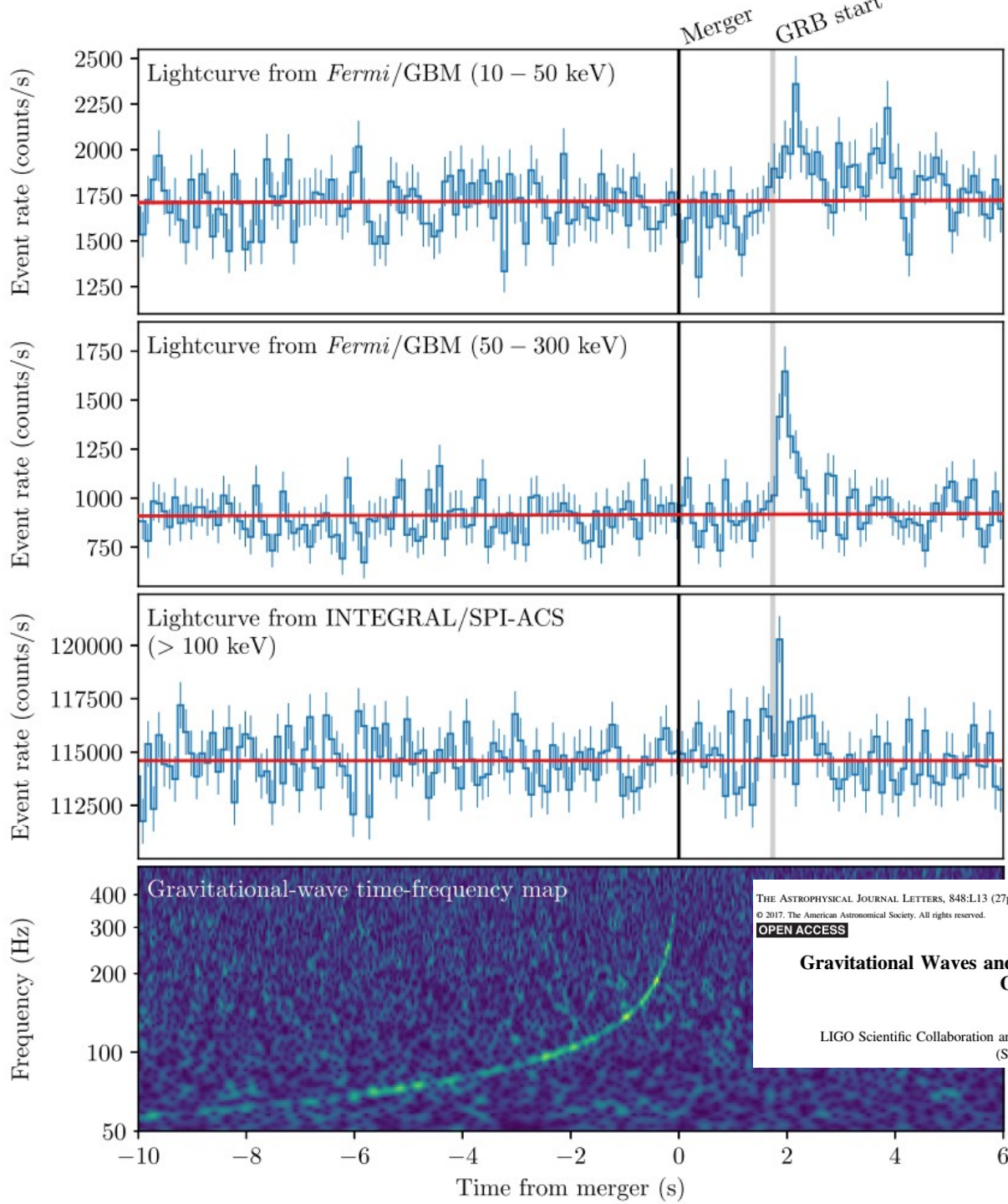
• w świetle widzialnym

• w podczerwieni

• 5 artykułów w Nature  
• dedykowany numer ApJ  
• ponad 100 prac ukazało się  
17.10.2017







Joint  
multi-messenger  
detection of  
GW170817  
and  
GRB170817A

THE ASTROPHYSICAL JOURNAL LETTERS, 848:L13 (27pp), 2017 October 20

<https://doi.org/10.3847/2041-8213/aag920c>

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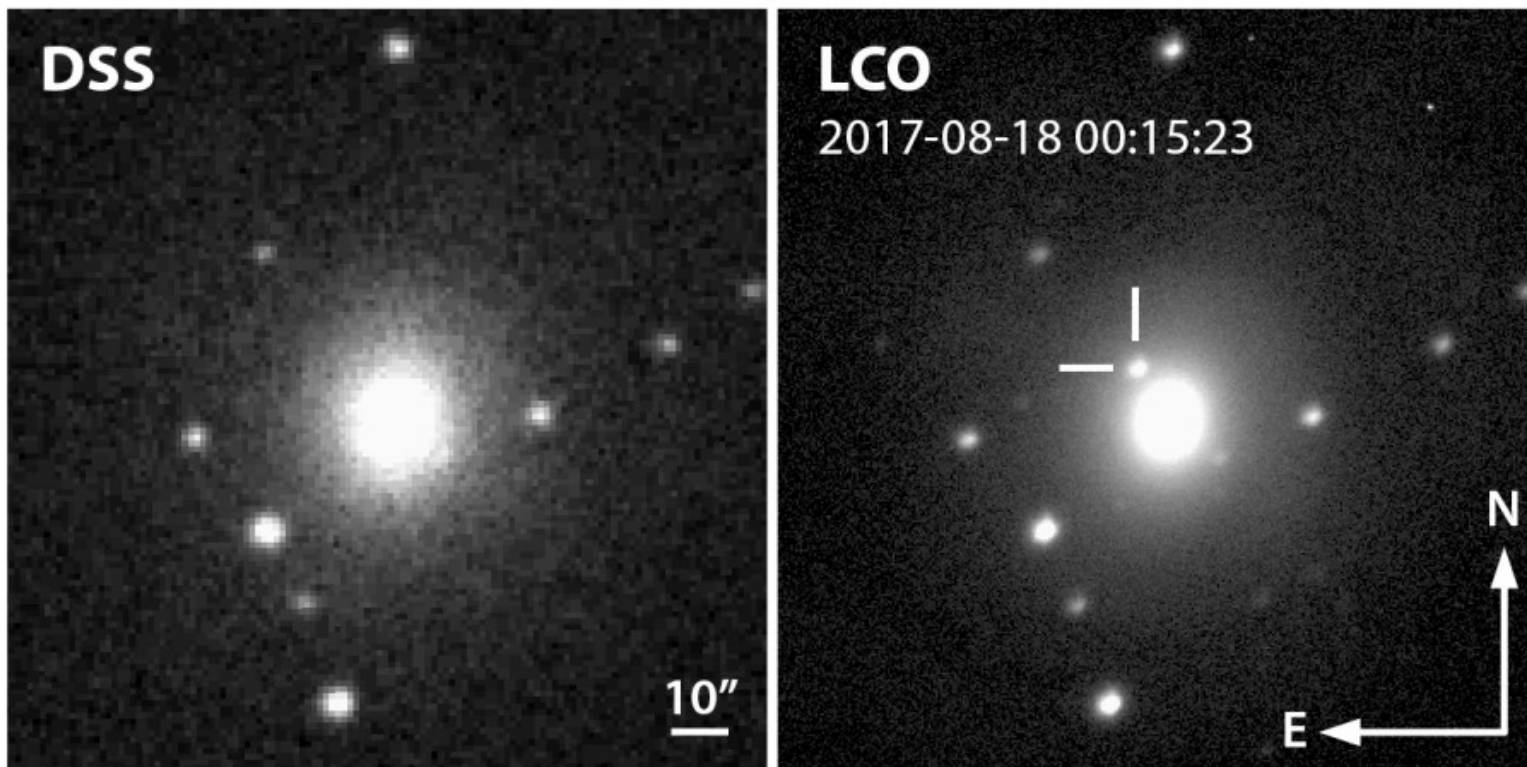
OPEN ACCESS



**Gravitational Waves and Gamma-Rays from a Binary Neutron Star Merger:  
GW170817 and GRB 170817A**

LIGO Scientific Collaboration and Virgo Collaboration, *Fermi* Gamma-ray Burst Monitor, and INTEGRAL  
(See the end matter for the full list of authors.)





**Figure 2 | LCO discovery image of the kilonova AT 2017gfo in the galaxy NGC 4993.** The *w*-band LCO image (right), centered on NGC 4993, clearly shows a new source (marked with white ticks) compared to an archival image (left) taken on 1992 April 9 with the RG610 filter as part of the AAO-SES survey, retrieved via the Digitized Sky Survey (DSS).

LCO – Las Cumbres Observatory; CTIO – Cerro Tololo Inter-American Observatory

# Einstein gravitational wave Telescope

## Conceptual Design Study

Polskie Konsorcjum  
Teleskopu Einsteina



## Co dalej?

# Teleskop Einsteina

- Czulość przewyższająca LIGO II generacji
- Potężne katalogi zjawisk w skalach kosmologicznych

$10^3 - 10^8$  zjawisk rocznie !  
Odległość do 2 Gpc ( $z=17$ )

- Duże nadzieje
- Obecnie w fazie badań lokalizacyjnych

Niektóre z tych sygnałów  
będą soczewkowane

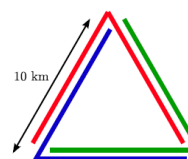


Figure 6: Three nested detectors in a triangular arrangement will form the final Einstein Telescope geometry.



# Przewidywania częstości soczewkowanych sygnałów grawitacyjnych

**J**ournal of **C**osmology and **A**stroparticle **P**hysics  
An IOP and SISSA journal

## Strong gravitational lensing of gravitational waves in Einstein Telescope

Aleksandra Piórkowska,<sup>a</sup> Marek Biesiada<sup>a</sup> and Zong-Hong Zhu<sup>b</sup>

<sup>a</sup>Department of Astrophysics and Cosmology, Institute of Physics, University of Silesia, Uniwersytecka 4, 40-007 Katowice, Poland

<sup>b</sup>Department of Astronomy, Beijing Normal University, Beijing 100875, China

**J**ournal of **C**osmology and **A**stroparticle **P**hysics  
An IOP and SISSA journal

## Strongly lensed gravitational waves from intrinsically faint double compact binaries — prediction for the Einstein Telescope

Xuheng Ding,<sup>a</sup> Marek Biesiada<sup>a,b,c</sup> and Zong-Hong Zhu<sup>a</sup>

<sup>a</sup>Department of Astronomy, Beijing Normal University, Beijing 100875, China

<sup>b</sup>Department of Astrophysics and Cosmology, Institute of Physics, University of Silesia, Uniwersytecka 4, 40-007 Katowice, Poland

<sup>c</sup>Kavli Institute for Theoretical Physics China, CAS, Beijing 100190, China

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X. Ding *et al.* JCAP12(2015)006

50 – 100 rocznie

JCAP12(2015)

A. Piórkowska *et al.* JCAP10(2013)02:

**J**ournal of **C**osmology and **A**stroparticle **P**hysics  
An IOP and SISSA journal

## Strong gravitational lensing of gravitational waves from double compact binaries — perspectives for the Einstein Telescope

Marek Biesiada,<sup>a,b</sup> Xuheng Ding,<sup>a</sup> Aleksandra Piórkowska<sup>b</sup> and Zong-Hong Zhu<sup>a</sup>

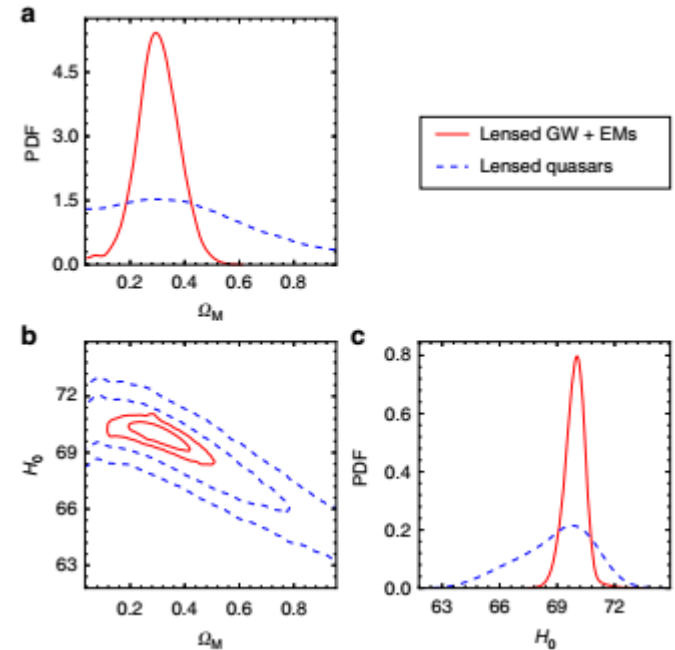
M. Biesiada *et al.* JCAP10(2014)080

# Precision cosmology from future lensed gravitational wave and electromagnetic signals

Kai Liao<sup>1,2</sup>, Xi-Long Fan<sup>3</sup>, Xuheng Ding<sup>1,4,5</sup>, Marek Biesiada<sup>4,6</sup> & Zong-Hong Zhu<sup>1,4</sup>

Wielka precyzja pomiaru opóźnień czasowych między obrazami będzie przełomowa !

The standard siren approach of gravitational wave cosmology appeals to the direct luminosity distance estimation through the waveform signals from inspiralling double compact binaries, especially those with electromagnetic counterparts providing redshifts. It is limited by the calibration uncertainties in strain amplitude and relies on the fine details of the waveform. The Einstein telescope is expected to produce  $10^4$ - $10^5$  gravitational wave detections per year, 50-100 of which will be lensed. Here, we report a waveform-independent strategy to achieve precise cosmography by combining the accurately measured time delays from strongly lensed gravitational wave signals with the images and redshifts observed in the electromagnetic domain. We demonstrate that just 10 such systems can provide a Hubble constant uncertainty of 0.68% for a flat lambda cold dark matter universe in the era of third-generation ground-based detectors.



**Table 2 The average constraining power of 10 lensed gravitational wave + electromagnetic systems**

|             | Flat $\Lambda$ CDM<br>( $\Omega_M$ fixed) | Flat $\Lambda$ CDM |            | Flat $\omega$ CDM |            |     | Open $\Lambda$ CDM |            |            |
|-------------|---|--------------------|------------|-------------------|------------|-----|--------------------|------------|------------|
|             | $H_0$                                     | $H_0$              | $\Omega_M$ | $H_0$             | $\Omega_M$ | $w$ | $H_0$              | $\Omega_M$ | $\Omega_k$ |
| Uncertainty | 0.37%                                     | 0.68%              | 27%        | 2.2%              | 36%        | 25% | 1%                 | 38%        | $\pm 0.18$ |

We concern cosmological parameters in different scenarios: flat lambda cold dark matter (Flat  $\Lambda$ CDM) with or without dimensionless matter density  $\Omega_M$  fixed, flat  $\omega$ CDM where the dark energy equation of state  $\omega$  is a free parameter, and open  $\Lambda$ CDM where cosmic curvature  $\Omega_k$  is a free parameter. For the same number of lensed quasars, the power is weaker by a factor of  $\sim 4$  according to the uncertainty propagation using Eq. (1) and Table 1



## Speed of Gravitational Waves from Strongly Lensed Gravitational Waves and Electromagnetic Signals

Xi-Long Fan,<sup>1,2,\*</sup> Kai Liao,<sup>3</sup> Marek Biesiada,<sup>4,5</sup> Aleksandra Piórkowska-Kurpas,<sup>4</sup> and Zong-Hong Zhu<sup>1,5,†</sup>

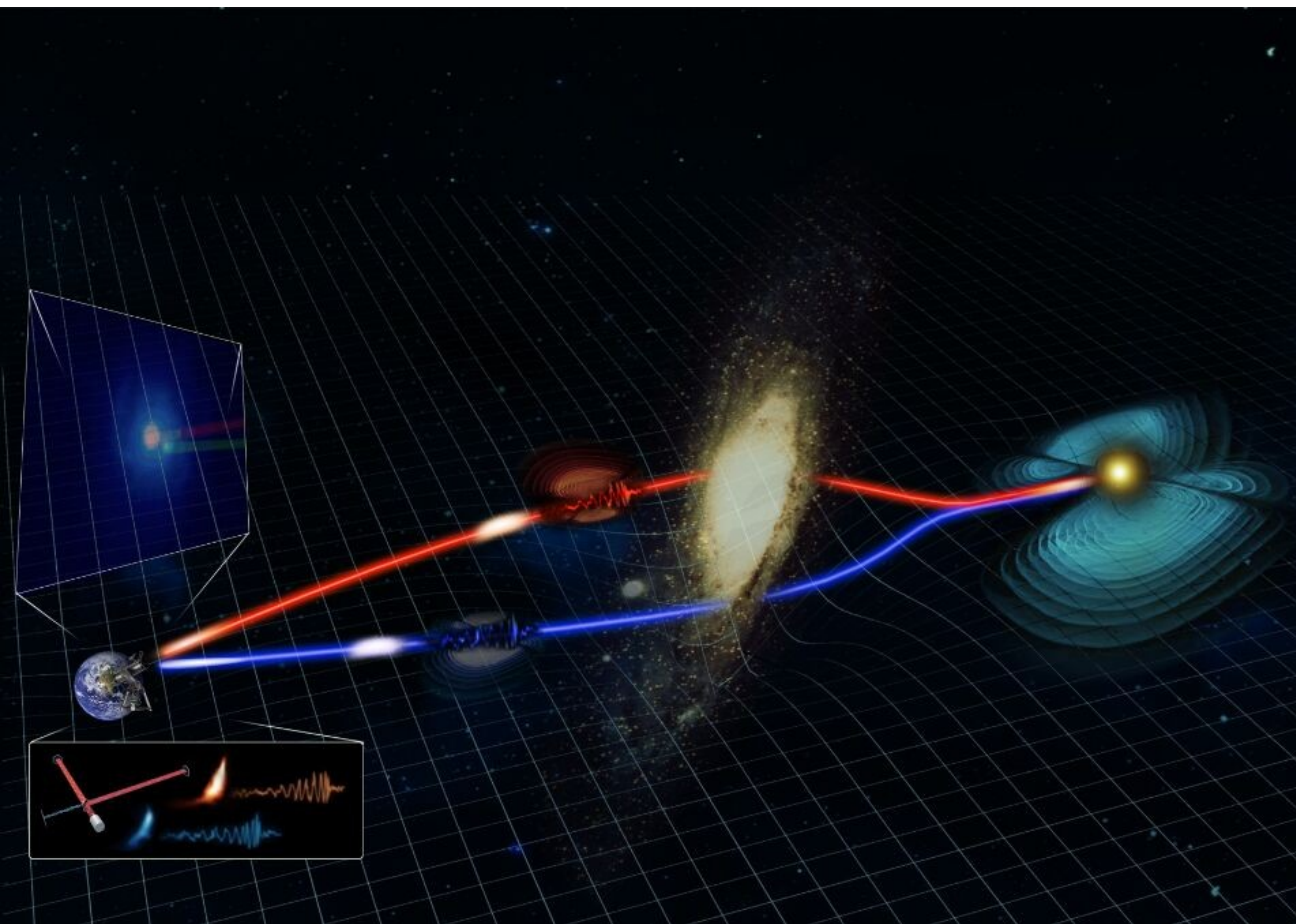
<sup>1</sup>*School of Physics and Technology, Wuhan University, Wuhan 430072, China*

<sup>2</sup>*Departments of Physics and Mechanical & Electrical Engineering, Hubei University of Education, Wuhan 430205, China*

<sup>3</sup>*School of Science, Wuhan University of Technology, Wuhan 430070, China*

<sup>4</sup>*Department of Astrophysics and Cosmology, Institute of Physics, University of Silesia, Uniwersytecka 4, 40-007 Katowice, Poland*

<sup>5</sup>*Department of Astronomy, Beijing Normal University, Beijing 100875, China*



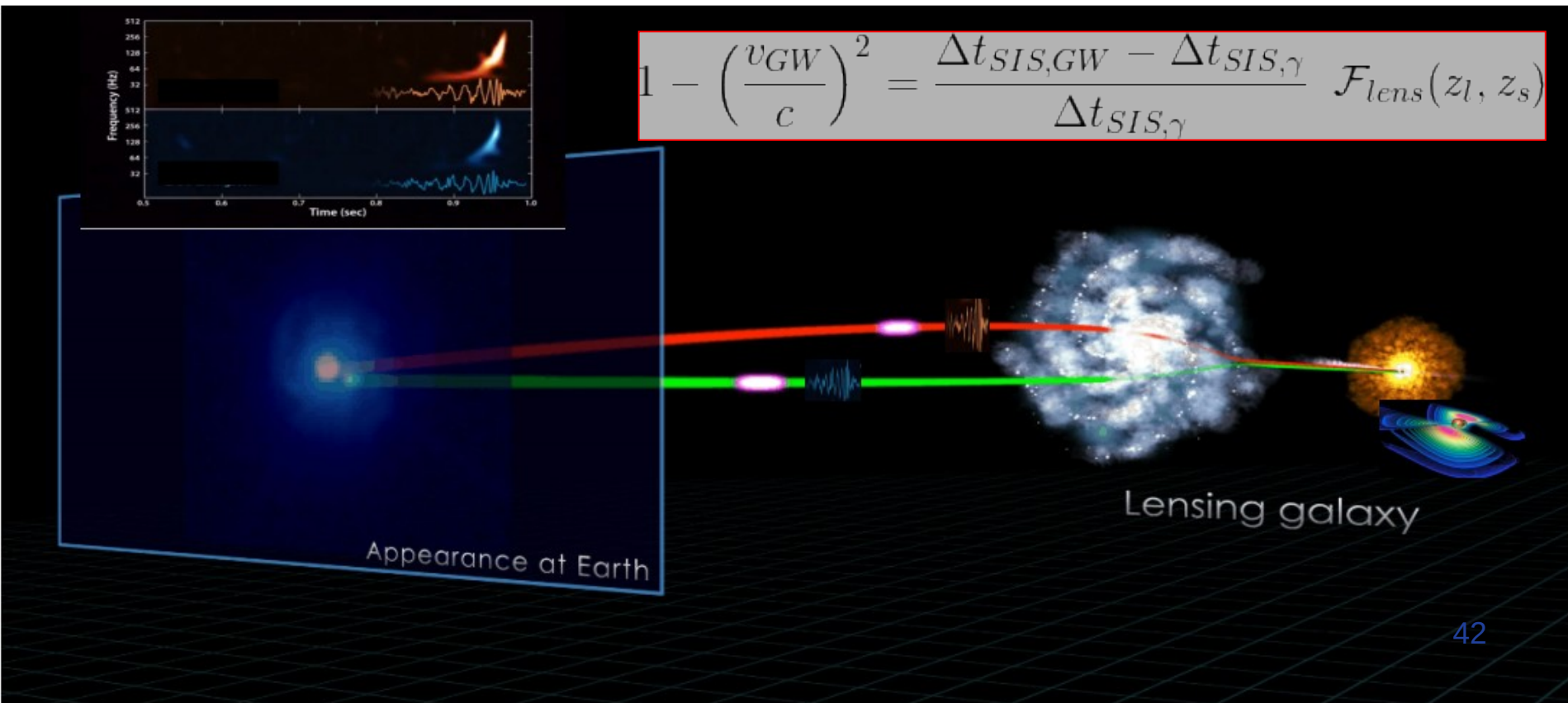
Różnice w opóźnieniach czasowych między soczewkowanym sygnałem EM i GW pozwolą testować prędkość propagacji fal grawitacyjnych

# Idea

OTW - fale grawitacyjne (GW) rozchodzą się z prędkością światła  $c$ , w zmodyfikowanych teoriach grawitacji mogą się propagować z inną prędkością  $v_{GW}$  (różną od  $c$ )

Opóźnienia czasowe  $\Delta t_{GW}$  między soczewkowanymi sygnałami grawitacyjnymi oraz odpowiednimi sygnałami świetlnymi (EM)  $\Delta t_{\gamma}$  będą różne

Metoda jest **wolna** od założeń odnośnie czasu emisji GW i EM ze źródła



# Reinterpreting Low Frequency LIGO/Virgo Events as Magnified Stellar-Mass Black Holes at Cosmological Distances.

arXiv: 1802.05273

Tom Broadhurst<sup>1,2</sup>, Jose M. Diego<sup>3</sup>, George Smoot III<sup>4,5,6</sup>

BH-BH zaobserwowane w LIGO miały duże masy, bo wszystkie były soczewkowane

Bardzo mało prawdopodobne ... !

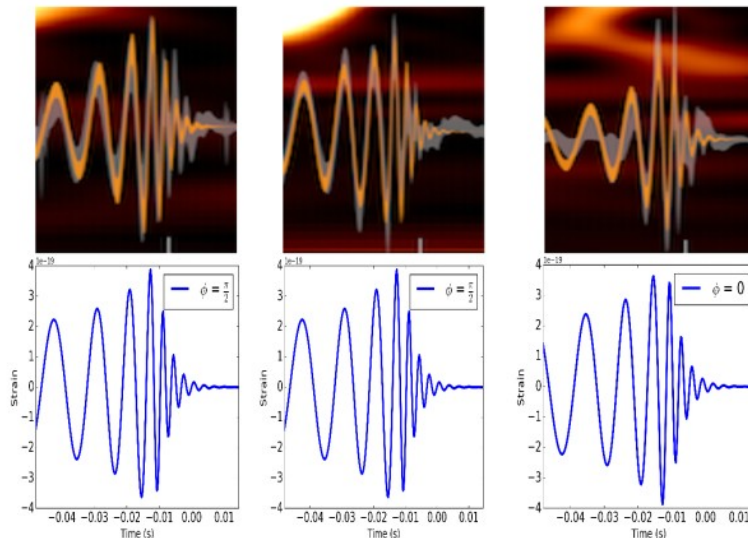
## Twin LIGO/Virgo Detections of a Viable Gravitationally-Lensed Black Hole Merger

arXiv: 1901.03190

Tom Broadhurst<sup>1,2,3</sup>, Jose M. Diego<sup>4</sup>, George F. Smoot<sup>5,6,7,8</sup>



Nagroda Nobla 2006



GW170809 i GW170814

to dwa silnie soczewkowane sygnały ...

Figure 1: **Phase similarity:** The similar pair of detected waveforms of interest here are shown for GW170809 and GW170814 in the left and middle panels respectively<sup>[1]</sup>. These are compared with model waveforms below showing that a fixed phase, defined with respect to the moment of merger shown underneath in blue, and fixed chirp mass of  $28.5M_{\odot}$  (in the detector frame)



# What if LIGO's gravitational wave detections are strongly lensed by massive galaxy clusters?

arXiv: 1707.03412

Graham P. Smith,<sup>1\*</sup> Mathilde Jauzac,<sup>2,3,4,5</sup> John Veitch,<sup>1,6,7</sup> Will M. Farr,<sup>1,7</sup>  
Richard Massey,<sup>2</sup> Johan Richard<sup>8</sup>

*Gravitational Waves Astrophysics: Early Results from GW Searches and Electromagnetic Counterparts*  
Proceedings IAU Symposium No. 338, 2018  
A.C. Editor, B.D. Editor & C.E. Editor, eds.

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DOI: 00.00

## Powtórka z supernowej Refsdala ?

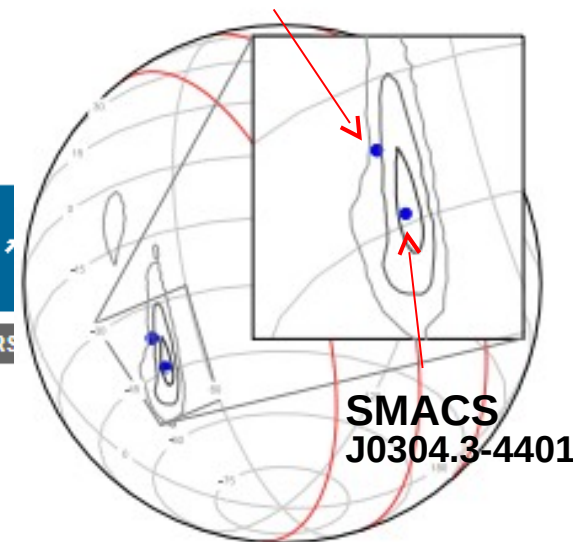
## Strong-lensing of Gravitational Waves by Galaxy Clusters

Graham P. Smith,<sup>1†</sup> Christopher Berry,<sup>1,2</sup> Matteo Bianconi,<sup>1</sup>  
Will M. Farr,<sup>1,2</sup> Mathilde Jauzac,<sup>3,4,5,6</sup> Richard Massey,<sup>3</sup>  
Johan Richard,<sup>7</sup> Andrew Robertson,<sup>4</sup> Keren Sharon,<sup>8</sup>  
Alberto Vecchio,<sup>1,2</sup> John Veitch.<sup>9</sup>

arXiv: 1803.07851

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*Birmingham, B15 2TT, England*  
*Université Laval Cedex, France*

Abell 3084



GW170814



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## GCN: The Gamma-ray Coordinates Network (TAN: Transient Astronomy Network)

TITLE: GCN CIRCULAR NUMBER: 21692

SUBJECT: LIGO/Virgo G297595: Gemini and VLT observations by GLGW Hunters

DATE: 17/08/25 14:18:20 GMT

FROM: Graham P Smith at U of Birmingham <gps@star.sr.bham.ac.uk>

G. P. Smith (Birmingham), M. Jauzac (Durham), M. Bianconi (Birmingham), J. Richard (Lyon),

C. P. L. Berry (Birmingham), W. M. Farr (Birmingham), R. Massey (Durham), A. Robertson (Durham),

K. Sharon (Michigan), A. Vecchio (Birmingham), J. Veitch (Glasgow)

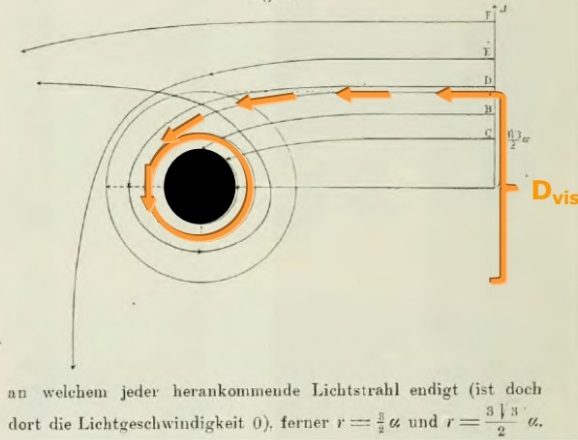
## The Gravitationally-lensed Gravitational Wave Hunters collaboration

report observations of strong-lensing galaxy clusters located within the sky localisation of the LIGO/Virgo trigger G297595 (LVC GCN Circ. 21474).



Daraus ziehen wir in Anlehnung an Poincarés Zykelttheorie den überdies recht anschaulichen Schluß: Der Lichtstrahl, der im Unendlichen auf den Abstand  $\mathcal{A} = \frac{3\sqrt{3}}{2}\alpha$  hinzielt, biegt sich nach innen und nähert sich auf einer Spirale asymptotisch dem Kreise  $r = \frac{3}{2}\alpha$ . Dann ergibt sich für die Gesamtheit der betrachteten Strahlen die Fig. 23. Sie zeigt uns die Kreise  $r = \alpha$ ,

Fig. 23.



an welchem jeder herankommende Lichtstrahl endigt (ist doch dort die Lichtgeschwindigkeit 0), ferner  $r = \frac{3}{2}\alpha$  und  $r = \frac{3\sqrt{3}}{2}\alpha$ .

**Max von Laue (1921):**  
 "Die Relativitätstheorie. Zweiter Band", Vieweg, 1921

stabe der  $r$ , zwischen  $\alpha$  und  $\frac{3}{2}\alpha$  liegt, so vergrößert, daß sie ihm den Halbmesser  $\frac{3\sqrt{3}}{2}\alpha$  zu haben scheint. Überhaupt alle Kugeln werden optisch vergrößert. Die im Text folgende Rechnung gibt für die rela-

Based on **David Hilbert (1916)**: lectures, "Die Grundlagen der Physik"

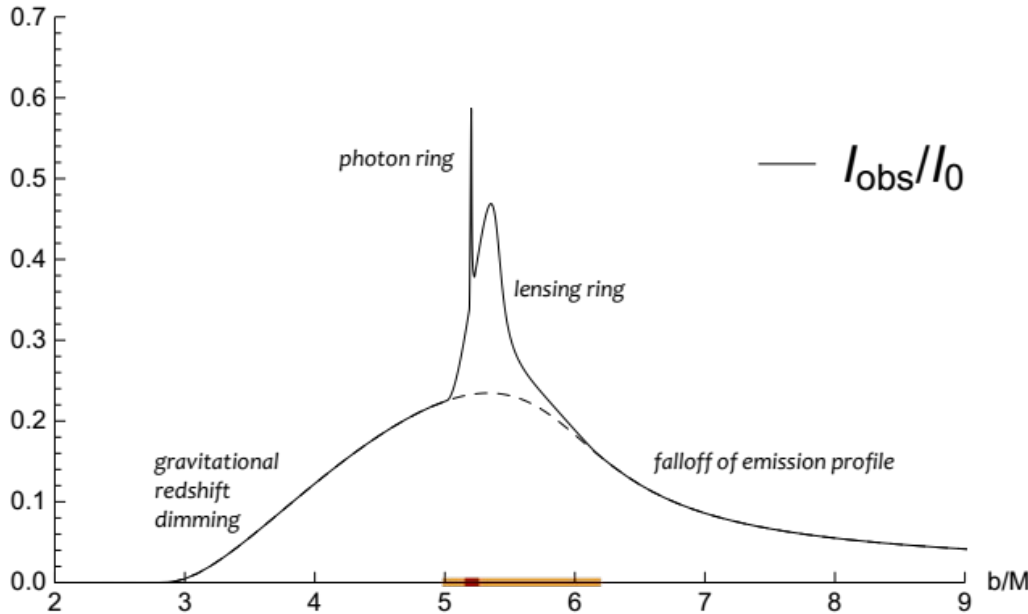
Black Hole "photon orbit":

$$R_{ph} = \frac{3}{2}R_S$$

Black Hole "cross section":

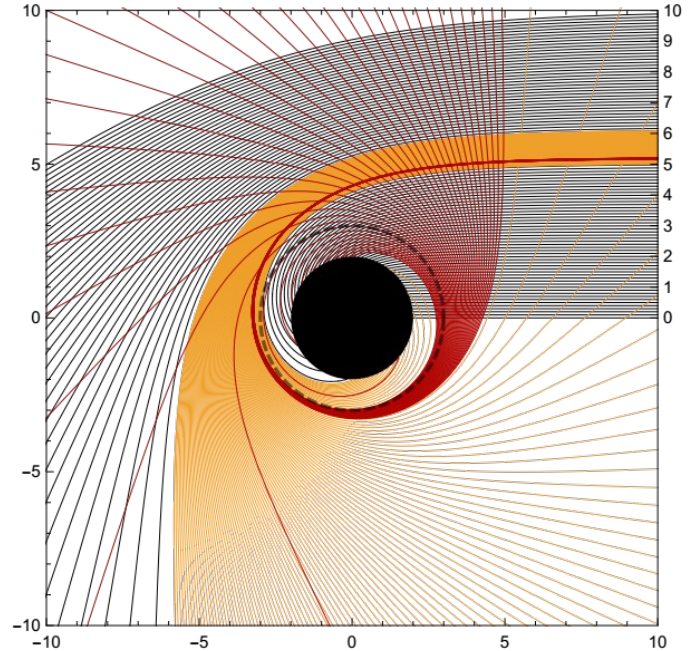
$$D = 3\sqrt{3}R_S \sim 5.2R_S$$

Credit: Heino Falcke "Imagining black holes"



Ekstremalny przypadek soczewkowania grawitacyjnego

Obraz horyzontu czarnej dziury



Credit: S.E. Gralla, D.E. Holz, R.W. Wald arXiv:1906.00873



# First M87 Event Horizon Telescope Results. I. The Shadow of the Supermassive Black Hole

The Event Horizon Telescope Collaboration  
(See the end matter for the full list of authors.)

Received 2019 March 1; revised 2019 March 12; accepted 2019 March 12; published 2019 April 10

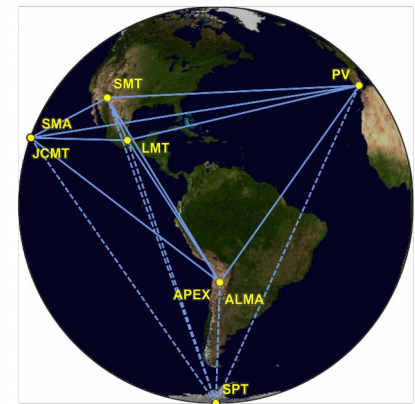
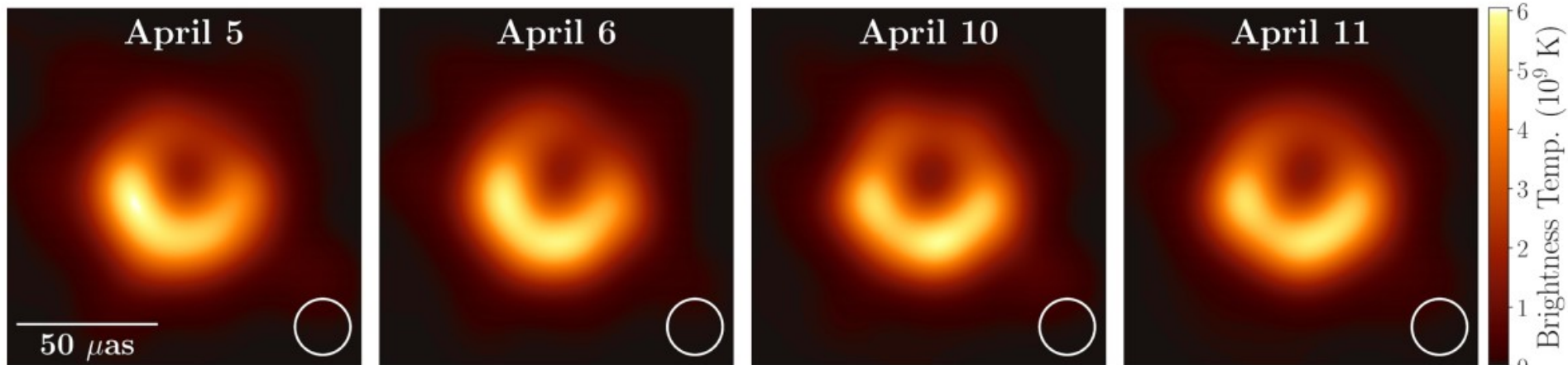
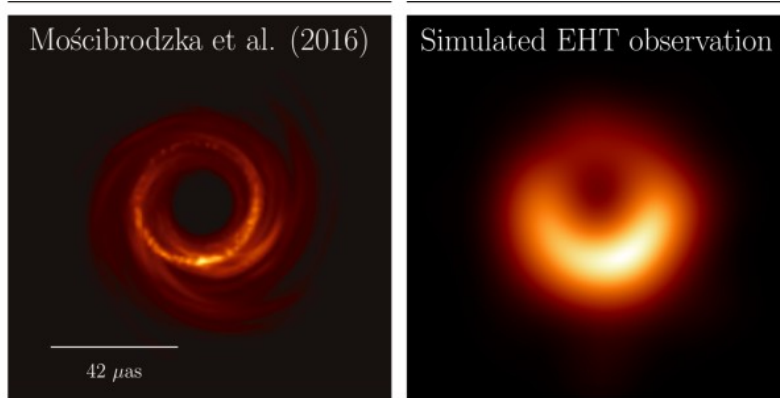


Figure 1. Eight stations of the EHT 2017 campaign over six geographic locations as viewed from the equatorial plane. Solid baselines represent mutual visibility on M87\* (+12° declination). The dashed baselines were used for the calibration source 3C279 (see Papers III and IV).

Monika Mościbrodzka  
Maciej Wielgus

Table 1  
Parameters of M87\*

| Parameter                          | Estimate                              |
|------------------------------------|---------------------------------------|
| Ring diameter <sup>a</sup> $d$     | $42 \pm 3 \mu\text{as}$               |
| Ring width <sup>a</sup>            | $< 20 \mu\text{as}$                   |
| Crescent contrast <sup>b</sup>     | $> 10:1$                              |
| Axial ratio <sup>a</sup>           | $< 4:3$                               |
| Orientation PA                     | $150^\circ - 200^\circ$ east of north |
| $\theta_g = GM/Dc^2$ <sup>c</sup>  | $3.8 \pm 0.4 \mu\text{as}$            |
| $\alpha = d/\theta_g$ <sup>d</sup> | $11^{+0.5}_{-0.3}$                    |
| $M$ <sup>c</sup>                   | $(6.5 \pm 0.7) \times 10^9 M_\odot$   |



DZIĘKUJĘ ZA UWAGĘ !

